

ÇÖZÜMLER

1.
$$\begin{aligned} \frac{4}{3} - \frac{\frac{3}{2}}{2 - \frac{1}{2}} &= \frac{4}{3} - \frac{\frac{3}{2}}{\frac{3}{2}} \\ &= \frac{4}{3} - 1 \\ &= \frac{1}{3} \text{ bulunur.} \end{aligned}$$

2.
$$\begin{aligned} \frac{0,15}{0,2 + \frac{0,3}{0,75}} &= \frac{\frac{15}{100}}{\frac{2}{10} + \frac{30}{75}} \\ &= \frac{\frac{15}{100}}{\frac{1}{5} + \frac{6}{15}} \\ &= \frac{\frac{15}{100}}{\frac{5}{100}} = \frac{5}{2} \\ &= \frac{25}{100} = 0,25 \end{aligned}$$

3.
$$\begin{aligned} \frac{6^4 - 4^2}{2^{10} - 2^9 + 2^7} &= \frac{2^4 \cdot 3^4 - 2^4}{2^7(2^3 - 2^2 + 1)} \\ &= \frac{2^4(3^4 - 1)}{2^7 \cdot (5)} \\ &= \frac{80}{40} = 2 \end{aligned}$$

Cevap: B

4.
$$\begin{aligned} \frac{\sqrt{128} - \sqrt{8}}{\sqrt{3}(\sqrt{48} - \sqrt{12})} \\ &= \frac{\sqrt{64 \cdot 2} - \sqrt{4 \cdot 2}}{\sqrt{3}(\sqrt{16 \cdot 3} - \sqrt{4 \cdot 3})} \\ &= \frac{8\sqrt{2} - 2\sqrt{2}}{\sqrt{3}(4\sqrt{3} - 2\sqrt{3})} \\ &= \frac{6\sqrt{2}}{\sqrt{3} \cdot (2\sqrt{3})} = \frac{6\sqrt{2}}{6} \\ &= \sqrt{2} \end{aligned}$$

Cevap: A

TASARIM EĞİTİM YAYINLARI

5.
$$\begin{aligned} \frac{8! - 7!}{6!} - \frac{5! - 4!}{3!} \\ &= \frac{6!(8 \cdot 7 - 7)}{6!} - \frac{3!(5 \cdot 4 - 4)}{3!} \\ &= (56 - 7) - (20 - 4) \\ &= 49 - 16 \\ &= 33 \text{ bulunur.} \end{aligned}$$

Cevap: D

Cevap: B

6.
$$\begin{aligned} \sqrt[3]{x+1} - \sqrt[3]{27x+27} + \sqrt[3]{64x+64} &= 8 \\ \sqrt[3]{x+1} - 3\sqrt[3]{3^3(x+1)} + 3\sqrt[3]{4^3(x+1)} &= 8 \\ \sqrt[3]{x+1} - 3\sqrt[3]{(x+1)} + 4\sqrt[3]{(x+1)} &= 8 \\ 2\sqrt[3]{x+1} &= 8 \\ (\sqrt[3]{x+1})^3 &= (4)^3 \\ x+1 &= 64 \\ x &= 63 \text{ bulunur.} \end{aligned}$$

Cevap: D

Cevap: B

7.
$$\frac{ab^3 + a^2}{ab + b - a - 1} : \frac{a + b^2}{b - 1}$$

$$= \frac{ab(b^2 + a)}{b(a+1) - (a+1)} \cdot \frac{b-1}{a+b^2}$$

$$= \frac{ab}{(a+1)(b-1)} \cdot \frac{(b-1)}{1}$$

$$= \frac{ab}{a+1}$$

Cevap: E

8. * (4, a) $\rightarrow 4^{a+1} = 64$
 $4^{a+1} = 4^3$
 $a+1 = 3 \Rightarrow a = 2$

(4, 2) $\rightarrow 5x + 3y = 20 + 6 = 26 = b$

* (c, d) $\rightarrow c^{d+1} = 1$ ve $d^{c+1} = 25$
 $d^{c+1} = 5^2$
 $c+1 = 2$
 $c = 1$ ve $d = 5$

* (3, e) $\rightarrow 3^{e+1} \rightarrow e^{3+1} = f \rightarrow 27$
 $5x + 3y = 27$
 $\downarrow \quad \downarrow$
 $3 \quad 4$
 $e = 4$ olur.

$f - e + a + b + c + d = 256 - 3 + 2 - 26 + 1 + 5$
 $= 234$ bulunur.

Cevap: C

9. $x - 2y = 6 \dots \dots \dots \text{(i)}$

$$\frac{3^x}{9^{2y}} = \frac{3^x}{3^{4y}} = 3^4$$

$$3^{x-4y} = 3^4$$

$$x - 4y = 4 \dots \dots \dots \text{(ii)}$$

i ve ii'den

$$\begin{array}{r} x - 2y = 6 \\ -1/ \quad x - 4y = 4 \\ \hline x - 2y = 6 \\ -x + 4y = -4 \\ \hline 2y = 2 \\ y = 1 \end{array}$$

bulunur.

Cevap: C

10. $\frac{(n+1)!}{(n-2)!} + \frac{n!}{(n-1)!} = 64$

$$\frac{(n+1).n.(n-1).(n-2)!}{(n-2)!} + \frac{n.(n-1)!}{(n-1)!} = 64$$
 $(n+1).n.(n-1) + n = 64$
 $n((n+1).(n-1) + 1) = 64$
 $n.(n^2 - 1 + 1) = 64$
 $n.n^2 = 64$
 $n^3 = 64$
 $n^3 = 4^3 \Rightarrow n = 4$ bulunur.

Cevap: A

11. $\frac{29}{x} + \frac{4x}{5} = \frac{47}{x} + \frac{3x}{10}$

$$\frac{4x}{5} - \frac{3x}{10} = \frac{47}{x} - \frac{29}{x}$$

$$(2)$$

$$\frac{8x - 3x}{10} = \frac{18}{x}$$

$$\frac{5x}{10} = \frac{18}{x}$$

$$x^2 = 36$$

$$x = \pm 6$$

$$x = 6$$
 bulunur.

Cevap: E

12. $gof(x) = g(f(x)) = 3f(x) + 4$

$$g(x) = 3x + 4$$

$$g(4) = 3.4 + 4 = 16$$

$$fog(x) = f(g(x)) = \frac{g(x)}{4} + 7$$

$$f(x) = \frac{x}{4} + 7$$

$$fog(4) = f(g(4)) = f(16)$$

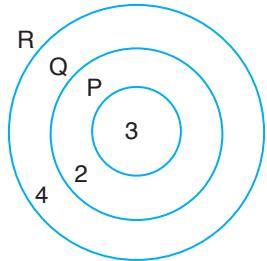
$$f(16) = \frac{16}{4} + 7$$

$$f(16) = 4 + 7 = 11$$

Cevap: E

13. * $f(2x + 3) = -5x + 2a - 1$
 $x = -1$ için
 $f(-2 + 3) = -5 \cdot (-1) + 2a - 1$
 $8 = 5 + 2a - 1$
 $4 = 2a \Rightarrow a = 2$
 $f(2x + 3) = -5x + 4 - 1$
 $f(2x + 3) = -5x + 3$
 $x = 1$ için
 $f(5) = -5 + 3$
 $f(5) = -2$ bulunur.

14. $P \subset Q \subset R$
 $n(P) = 3, n(Q) = 5, n(R) = 9$



$$n(P \cup Q) + n(P \cap R) = 5 + 3 = 8$$

15. $(8,3 + 4,3)^2 - 4 \cdot (8,3) - (4,3)$
 $a = 8,3, b = 4,3$
 $= (a + b)^2 - 4ab$
 $= a^2 + 2ab + b^2 - 4ab$
 $\Rightarrow a^2 - 2ab + b^2 = (a - b)^2$
 $(8,3 - 4,3)^2 = (4)^2 = 16$ bulunur.

16. $24 \div 6 = 4$ $8 \times 7 = 56$ $28 - 7 = 21$
 $4 \times 5 = 20$ $456 - 6 = 50$ $21 \div 3 = 50$
 $20 - 11 = 9$ $50 \div 10 = 5$ $7 \times 4 = 28$
 $\blacktriangle \rightarrow \div, \textcolor{blue}{*} \rightarrow \times, \textcolor{purple}{\bullet} \rightarrow -$
 $35 \div 5 = 7$
 $7 - 2 = 5$
 $5 \times 8 = 40$

Cevap: E

17. $5^{x+1} = 15^x$
 $5^x \cdot 5^1 = 3^x \cdot 5^x$
 $3^x = 5 \quad \text{ve} \quad 3^{x \cdot \frac{1}{x}} = 5^{\frac{1}{x}}$
O halde
 $9^x \cdot 5^x = (3^x)^2 \cdot 5^x$
 $= (5)^2 \cdot 3$
 $= 25 \cdot 3$
 $= 75$

Cevap: E

18. $A = \{x / 0 < x \leq 10 \quad x \in \mathbb{Z}^+\}$
 $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
 $B = \{y / y = 2k : 0 < k \leq 10 \quad x \in \mathbb{Z}^+\}$
 $B = \{2, 4, 6, 8, 10\}$
• $(A \cap B) = \{2, 4, 6, 8, 10\}$
 $n(A \cap B) = 5$

Cevap: B

TASARI EĞİTİM YAYINLARI

Cevap: C

19. $P(x) = ax^2 + bx + c$
 $P(1) = 0$
 $a + b + c = 0 \Rightarrow c = -a - b$
 $P(2) = 0$
 $4a + 2b + c = 0$
 $4a + 2b - a - b = 0$
 $3a + b = 0$
 $b = -3a$
 $\frac{b}{a} = -3$ bulunur.

Cevap: A**Cevap: B**

20. $P(x) = (x^2 - 16).Q(x) + 3x$

	$(x^2 - 16).Q(x) + 3x$	$\underline{(x+4)}$
-	$-(x^2 - 16.Q(x))$	$(x-4).Q(x) + 3$
	3x	
+	-/ 3x + 12	
		-12 bulunur.

Cevap: E**Cevap: E**

21. ABC C = 9

$$\begin{array}{r} + \quad A 4 \\ \hline C 0 3 \end{array}$$

 B = 1
 A = 8

$$\begin{array}{r} 8 1 9 \\ + \quad 8 4 \\ \hline 9 0 3 \end{array}$$

$$A \cdot B \cdot C = 8 \cdot 1 \cdot 9 = 72$$

22. $\left(x+3+\frac{3}{x+3}\right)^2 = (3+3)^2$
 $(x+3)^2 + \frac{9}{(x+3)^2} + 2 \cdot (x+3) \cdot \frac{3}{x+3} = 36$
 $(x+3)^2 + \frac{9}{(x+3)^2} = 36 - 6 = 30$

23. $|15-a| = 11+a$
 i) $15-a = 11+a$
 $4 = 2a$
 $2 = a$
 * $|x-2| = x-6$
 ii) $15-a = -11-a$
 $15 \neq -11$
 i) $x-2 = x-6$
 $2 \neq 6$
 ii) $x-2 = -x+6$
 $2x = 8$
 $x = 4$

24. $x^2 + (a+2)x + 8 = 0$
 $x_1^2 \cdot x_2 + x_2^2 \cdot x_1 = 16$
 $x_1 \cdot x_2 (x_1 + x_2) = 16$
 $\downarrow \quad \downarrow$
 $8 \cdot (-a-2) = 16$
 $-a-2 = 2$
 $-2-2 = a$
 $-4 = a$ bulunur.

Cevap: D

Cevap: C

Cevap: D

Cevap: A

25. $\left(\frac{1}{b}-\frac{1}{a}\right) \cdot \left(\frac{1}{b}+\frac{1}{a}\right) = \frac{6}{49}$
 $\left(\frac{1}{b}-\frac{1}{a}\right) \cdot \frac{6}{7} = \frac{6}{49}$

$$\begin{array}{r} \frac{1}{b}-\frac{1}{a} = \frac{1}{7} \\ + \quad \frac{1}{a}+\frac{1}{b} = \frac{6}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \frac{2}{b} = \frac{7}{7} = 1 \\ b = 2 \end{array}$$

$$\begin{array}{r} \frac{1}{2}+\frac{1}{a} = \frac{6}{7} \\ \frac{1}{a} = \frac{6}{7}-\frac{1}{2} = \frac{12-7}{14} = \frac{5}{14} \Rightarrow a = \frac{14}{5} \\ \Rightarrow a \cdot b = \frac{14}{5} \cdot 2 = \frac{28}{5} \text{ bulunur.} \end{array}$$

Cevap: D

TASARI EĞİTİM YAYINLARI

26. $x-y=12$
 $-1/y+z=8$
 $-2/z-v=5$

$$\begin{array}{r} x-y=12 \\ -y-z=-8 \\ + -2z+2v=-10 \\ \hline x-2y-3z+2v=-6 \text{ bulunur.} \end{array}$$

Cevap: B

27. $\frac{5}{x} = \frac{7}{y} = \frac{1}{k} \Rightarrow x=5k$
 $y=7k$ alınabilir.
 $x^2+y^2=(5k)^2+(7k)^2=148$
 $25k^2+49k^2=148$
 $74k^2=148$
 $k^2=2$
 $k=\sqrt{2}$
 $x+y=5k+7k=12k=12\sqrt{2}$

Cevap: C

28. $|a+2|=7$ $|b-4|=5$

$$\begin{array}{l} \downarrow \\ a+2=7 \text{ ve } a+2=-7 \\ a=5 \quad a=-9 \end{array} \quad \begin{array}{l} \downarrow \\ b-4=5 \text{ ve } b-4=-5 \\ b=9 \quad b=-1 \end{array}$$

$a+b$ toplamının en büyük olabilmesi için
 $a=5$ ve $b=9$ alınır.

$\text{Max}(a+b) = 5 + 9 = 14$ bulunur.

29. $z < y < x$ olduğuna göre

$$\frac{x}{y} + z = 8, \quad z = 1, \quad y = 2 \text{ seçilirse}$$

$$\frac{x}{2} + 1 = 8$$

$$\frac{x}{2} = 7 \Rightarrow x = 14$$

$x.z = 14.1 = 14$ bulunur.

30. $(97)_{10} = (241)_m$
 $97 = 2m^2 + 4.m + 1$
 $96 = 2m(m+2)$
 $48 = m.(m+2)$
 $6 \quad 8$
 $m = 6$ bulunur.

Cevap: C

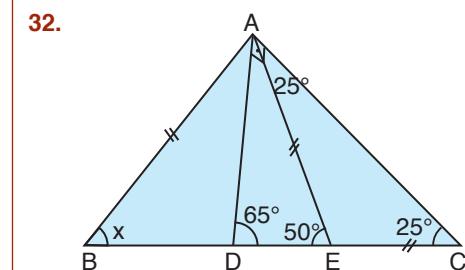
31. $3^a \cdot 4^{-b} = 4$
 $x \quad 3^{-b} \cdot 4^a = 36$

$$\begin{aligned} 3^{a-b} \cdot 4^{a-b} &= 4 \cdot 4 \cdot 9 \\ 3^{a-b} \cdot 4^{a-b} &= 4^2 \cdot 3^2 \\ 12^{a-b} &= 12^2 \\ a-b &= 2 \text{ bulunur.} \end{aligned}$$

Cevap: D

Cevap: E

Cevap: C

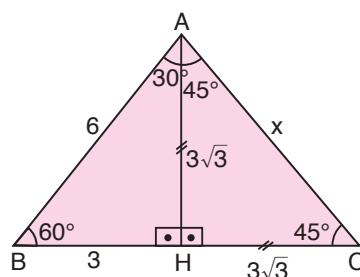


$$\begin{aligned} m(\widehat{ADC}) + m(\widehat{ACD}) &= 90^\circ \\ 65^\circ + m(\widehat{ACD}) &= 90^\circ \\ m(\widehat{ACD}) &= 90^\circ - 65^\circ = 25^\circ \\ |AE| &= |EC| \text{ olduğundan } m(\widehat{EAC}) = 25^\circ \\ m(\widehat{AEB}) &= 50^\circ \\ |AB| &= |AE| \text{ olduğundan} \\ m(\widehat{ABC}) &= 50^\circ \text{ bulunur.} \end{aligned}$$

Cevap: B

TASARI EĞİTİM YAYINLARI

33.



A noktasından [BC] kenarına dik çizersek,
ABH üçgeni($30^\circ, 60^\circ, 90^\circ$) dik üçgeni olur.

Bu durumda;

$$|AB| = 6 \text{ ise } |BH| = 3 \text{ ve } |AH| = 3\sqrt{3} \text{ olur.}$$

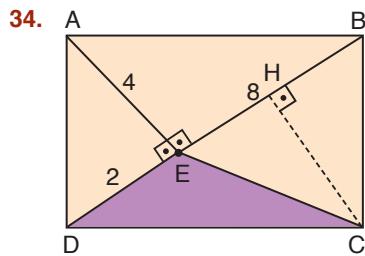
$$m(\widehat{HAC}) = 75 - 30 = 45^\circ \text{ bulunur.}$$

AHC ikizkenar dik üçgen olduğundan

Hipotenüs dik kenarın $\sqrt{2}$ katıdır.

$$x = 3\sqrt{3} \cdot \sqrt{2} = 3\sqrt{6} \text{ bulunur.}$$

Cevap: C



ABD üçgeninde öklid bağıntısından
 $|DE| \cdot 8 = 4^2$, $|DE| = 2$ cm olur.

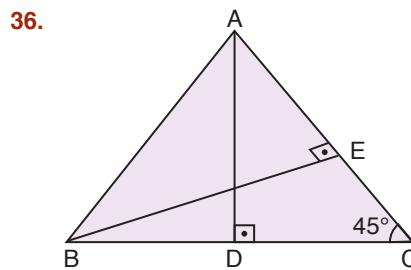
[CH] [DB] çizersek

DAB ile BCD eş üçgen olduğundan

$$|AE| = |CH| = 4 \text{ cm}$$

$$A(DEC) = \frac{|DE| \cdot |CH|}{2}$$

$$= \frac{2 \cdot 4}{2} = 4 \text{ cm}^2 \text{ olur.}$$



ABC üçgeninin alanını iki farklı şekilde yazıp eşitleyelim.

$$\frac{|BC| \cdot |AD|}{2} = \frac{|AC| \cdot |BE|}{2}$$

$$\frac{12 \cdot |AD|}{2} = \frac{16 \cdot 9}{2}$$

$$12 \cdot |AD| = 16 \cdot 9$$

$$|AD| = 12 \text{ cm bulunur.}$$

Cevap: D

Cevap: B

TASARI EĞİTİM YAYINLARI

35. Köşegenleri dik kesişen dörtgenlerde karşılıklı kenarların kareleri toplamı eşittir.

$$x^2 + 6^2 = 4^2 + 9^2$$

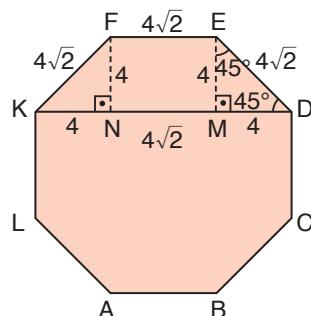
$$x^2 + 36 = 16 + 81$$

$$x^2 = 61$$

$$x = \sqrt{61} \text{ cm}$$

Cevap: A

37.



Düzenli sekizgenin bir iç açısı 135° ve KDEF ikizkenar yamuk olur.

$(45^\circ, 45^\circ, 90^\circ)$ ikizkenar dik üçgeninden

$$|EM| = |MD| = |KN| = |FN| = 4 \text{ cm olur.}$$

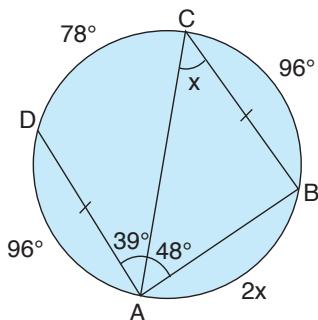
$$|ED| = |EF| = |NM| = 4\sqrt{2}$$

O halde

$$|KD| = 4 + 4\sqrt{2} + 4 = 8 + 4\sqrt{2} \text{ cm olur.}$$

Cevap: E

38.

 $|AD| = |BC|$ olduğundan $m(\widehat{DA}) = 96^\circ$ olur.

$$2x + 96 + 78 + 96 = 360$$

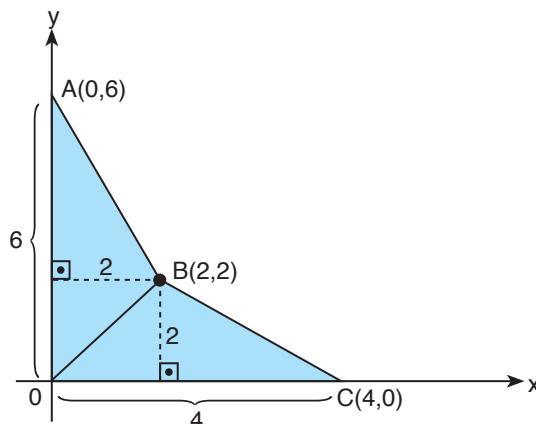
$$2x = 360 - 270$$

$$2x = 90^\circ$$

 $x = 45^\circ$ bulunur.

Cevap: C

40.

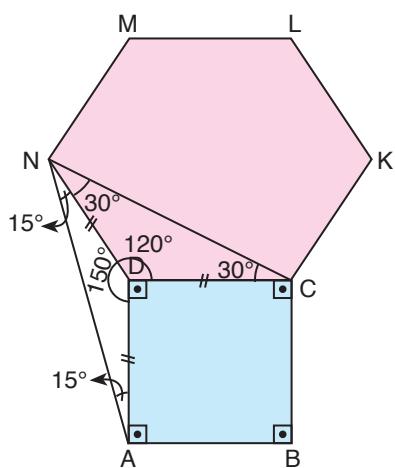


$$\begin{aligned} A(OBC) + A(OBA) &= \frac{4 \cdot 2}{2} + \frac{6 \cdot 2}{2} \\ &= 4 + 6 \\ &= 10 \text{ br}^2 \end{aligned}$$

Cevap: A

TASARIM EĞİTİM YAYINLARI

39.

Altigende köşe açıları 120° dir. $m(\widehat{NDC}) = 120^\circ$ $|ND| = |DC|$ olduğundan

NDC üçgeni ikizkenar olur.

 $m(\widehat{DNC}) = m(\widehat{DCN}) = 30^\circ$ $m(\widehat{NDA})$ açısı $120^\circ + 90^\circ + m(\widehat{NDA}) = 360^\circ$ $m(\widehat{NDA}) = 150^\circ$

NDA üçgeninin ikizkenar

 $m(\widehat{DNA}) = m(\widehat{DAN}) = 15^\circ$

O halde

 $m(\widehat{ANC}) = 15 + 30 = 45^\circ$ dir.

Cevap: C