

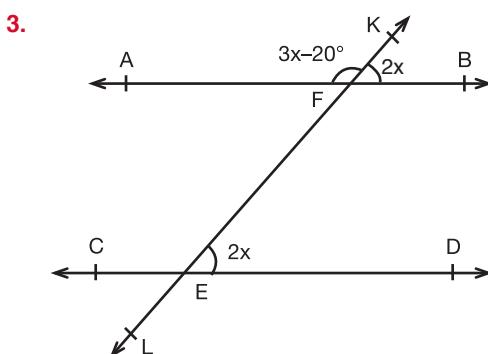
AÇI

$$\begin{aligned} 1. \quad 2.m(\widehat{A}) &= 72^\circ 84' 68'' = 71^\circ 144' 68'' \\ 3.m(\widehat{B}) &= 63^\circ 99' 63'' = 63^\circ 99' 63'' \\ 2m(\widehat{A}) - 3.m(\widehat{B}) &= 8^\circ 45' 05'' \end{aligned}$$

Cevap: A

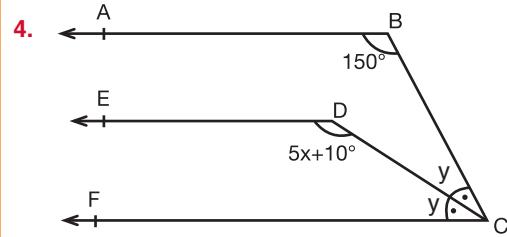
$$\begin{aligned} 2. \quad x + (6y - x) &= 90 \\ 6y &= 90 \\ y &= 15^\circ \end{aligned}$$

$$\begin{aligned} y + (5y + 2x) &= 180 \\ 6y + 2x &= 180 \\ 6.15 + 2x &= 180 \\ 2x &= 90 \\ x &= 45^\circ \\ x + y &= 45 + 15 = 60^\circ \end{aligned}$$



$$\begin{aligned} m(\widehat{FED}) &= m(\widehat{KFB}) \text{ (Yöndeş açılar)} \\ m(\widehat{KFA}) + m(\widehat{KFB}) &= 180^\circ \text{ (Bütünler açılar)} \\ 3x - 20 + 2x &= 180 \\ 5x &= 200 \\ x &= 40^\circ \\ m(\widehat{KFB}) &= 2x = 2.40 = 80 \end{aligned}$$

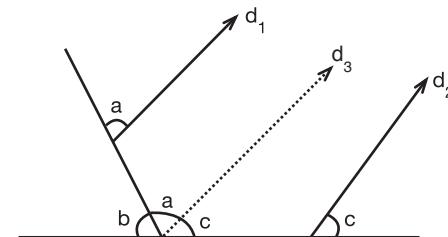
Cevap: E



$$\begin{aligned} m(\widehat{ABC}) + m(\widehat{BCF}) &= 180^\circ \text{ (Karşı durumlu açılar)} \\ 150 + 2y &= 180 \\ 2y &= 30 \\ y &= 15 \end{aligned}$$

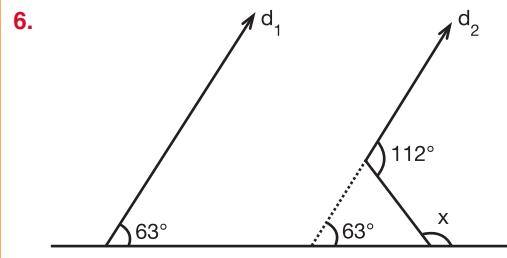
$$\begin{aligned} m(\widehat{EDC}) + m(\widehat{DCF}) &= 180^\circ \text{ (Karşı durumlu açılar)} \\ 5x + 10 + 15 &= 180 \\ 5x + 25 &= 180 \\ 5x &= 155 \\ x &= 31^\circ \end{aligned}$$

Cevap: C

TASARI & DEV KADRO
Cevap: C

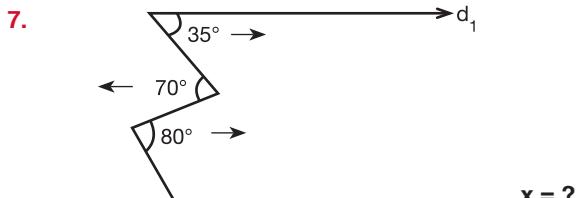
$$\begin{aligned} a + c &= 150 \\ a + b + c &= 180^\circ \\ a + c = 150^\circ &\Rightarrow b = 30^\circ \end{aligned}$$

Cevap: C



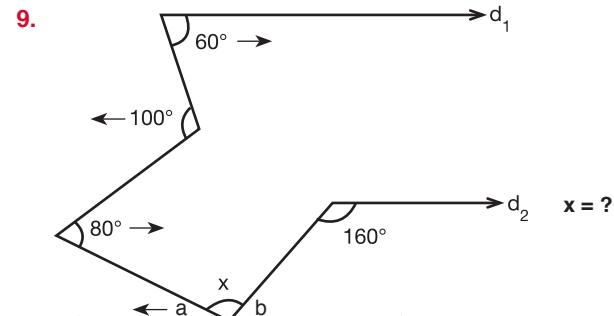
$$x = 68 + 63 = 131^\circ$$

Cevap: D



$$\begin{aligned} 35 + 80 &= 70 + (180 - 3x) \\ 115 &= 250 - 3x \\ 3x &= 135 \\ x &= 45^\circ \end{aligned}$$

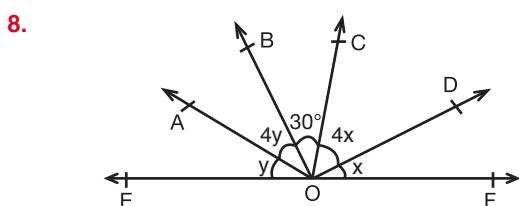
Cevap: D



$$\begin{aligned} 60 + 80 &= 100 + a & 160 + b &= 180^\circ \\ a &= 40^\circ & b &= 20^\circ \\ x + a + b &= 180^\circ \\ x + 40 + 20 &= 180^\circ & \Rightarrow & x = 120^\circ \end{aligned}$$

Cevap: B

TASARI & DEV KADRO



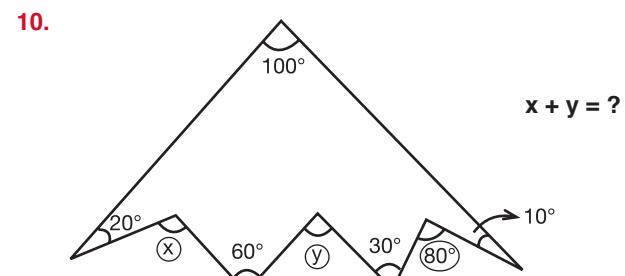
$$\begin{aligned} 4m(\widehat{FOD}) &= m(\widehat{COD}) \\ 4m(\widehat{EOA}) &= m(\widehat{AOB}) \end{aligned}$$

$$\begin{aligned} 5y + 30 + 5x &= 180 \\ 5(x + y) &= 150 \\ x + y &= 30 \end{aligned}$$

$$m(\widehat{AOD}) = ?$$

$$\begin{aligned} m(\widehat{AOD}) &= 4x + 4y + 30 \\ &= 4(x + y) + 30 \\ &= 4 \cdot 30 + 30 \\ &= 150 \end{aligned}$$

Cevap: D

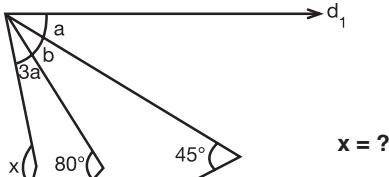


Kural: Şeklin içindeki açıların toplamı, dışındaki açıların toplamına eşittir.

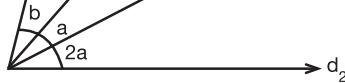
$$\begin{aligned} 100 + 20 + 60 + 30 + 10 &= x + y + 80 \\ x + y &= 140^\circ \end{aligned}$$

Cevap: A

11.



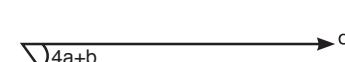
$x = ?$



$$\begin{aligned} a + 2a &= 45 \\ 3a &= 45 \\ a &= 15^\circ \end{aligned}$$



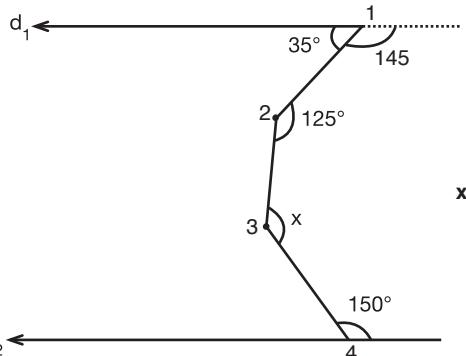
$$\begin{aligned} a + b + 3a &= 80 \\ 4a + b &= 80 \\ 4.15 + b &= 80 \\ b &= 20^\circ \end{aligned}$$



$$\begin{aligned} x &= 4a + b + 3a + b \\ x &= 7a + 2b \\ x &= 7.15 + 2.20 \\ x &= 105 + 40 \\ x &= 145^\circ \end{aligned}$$

Cevap: B

12.



$x = ?$

KURAL: İki paralel doğru arasında kalan ve aynı yöne bakan açıların toplamı:
(Kırık nokta sayısı - 1).180

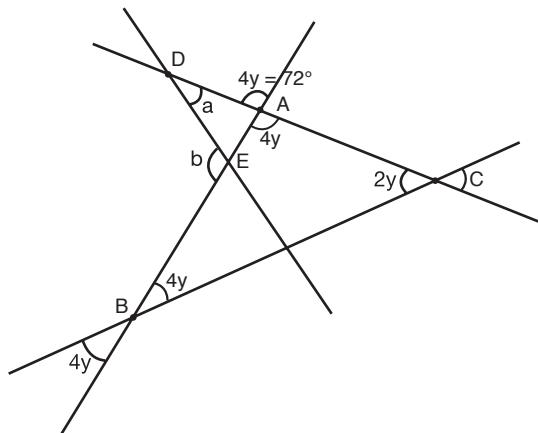
$$\begin{aligned} \text{Kırık nokta sayısı} &= 4 \\ x + 145 + 125 + 150 &= (4-1).180 \\ x &= 120 \end{aligned}$$

Cevap: C

TASARI & DEV KADRO

AÇI – ÜÇGENDE AÇI

1.



ABC üçgeninin iç açıları toplamı 180° olduğundan

$$4y + 4y + 2y = 180 \Rightarrow y = 18$$

$$4y = 72$$

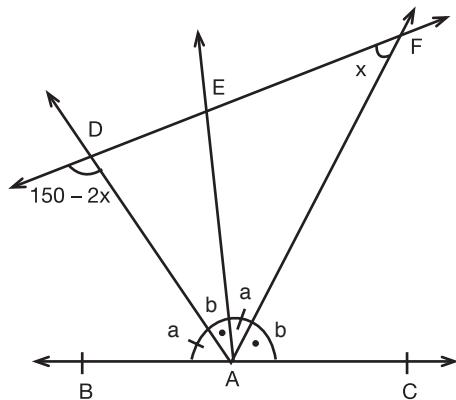
ADE üçgeninde iki iç açının toplamı kendilerine komşu olmayan bir dış açıya eşit olacağından,

$$a + 108 = b \Rightarrow b - a = 108^\circ \text{ dir.}$$

$$\begin{array}{r} b + a = 132 \\ + b - a = 108 \\ \hline 2b = 240 \end{array}$$

$$b = 120, a = 12^\circ \text{ dir.}$$

3.



$$2a + 2b = 180 \Rightarrow a + b = 90^\circ \text{ dir.}$$

$$m(\widehat{DAF}) = 90^\circ$$

$$x + 90 = 150 - 2x \quad (\widehat{DAF})$$

$$3x = 60$$

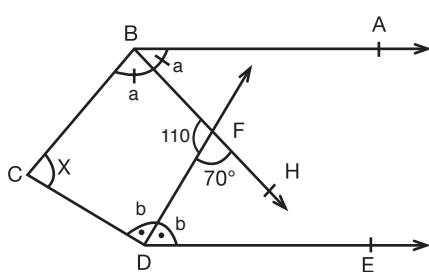
$$x = 20^\circ$$

Cevap: C

TASARI & DEV KADRO

Cevap: A

2.



$$2a + x + 2b = 360 \quad \text{ve} \quad a + b + x + 110 = 360$$

(-1 ile çarp)

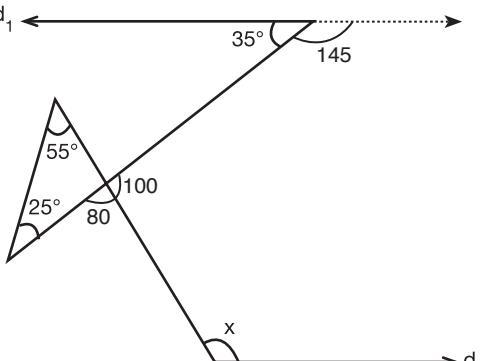
$$a + b + x = 250^\circ$$

(2 ile genişlet)

$$\begin{array}{r} 2a + 2b + 2x = 500 \\ + -2a - 2b - x = -360 \\ \hline x = 140 \end{array}$$

Cevap: E

4.

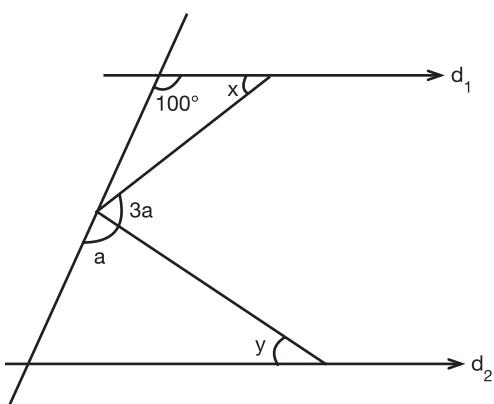


$$145 + 100 + x = 360 \Rightarrow x = 115^\circ$$

Cevap: C

AÇI – ÜÇGENDE AÇI

5.



$$3/x + 100 = 4a \Rightarrow 3x + 300 = 12a$$

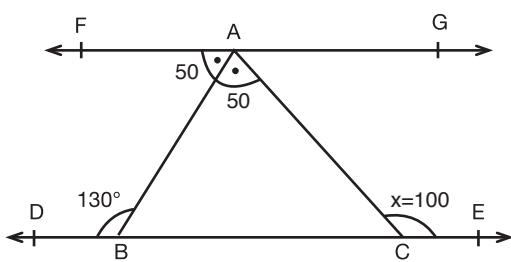
$$4/x + y = 3a \Rightarrow 4x + 4y = 12a$$

$$3x + 300 = 4x + 4y$$

$$x + 4y = 300$$

Cevap: D

6.

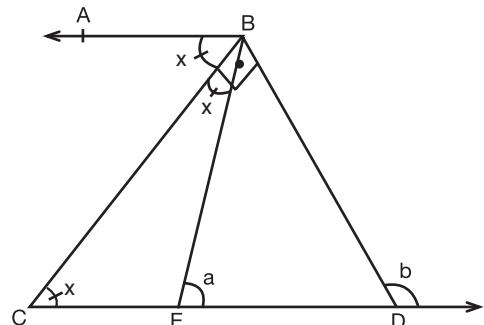


$$m(\widehat{FAB}) = 50 \text{ (Karşı durumlu açılar)}$$

$$m(\widehat{FAC}) = m(\widehat{ACE}) \text{ (İç ters açılar)}$$

Cevap: B

7.



$$b = 90 + x$$

$$x = b - 90$$

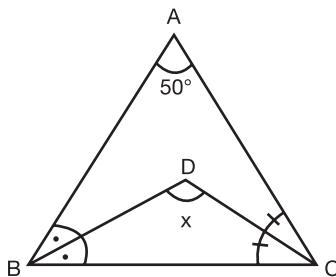
$$a = 2x$$

$$a = 2(b - 90)$$

$$a = 2b - 180$$

Cevap: A

8.



I. yol:

$$x = 90 + \frac{m(\widehat{A})}{2} \Rightarrow x = 90 + \frac{50}{2}$$

$$x = 115^\circ$$

II. yol:

$$50 + 2a + 2b = 180$$

$$2a + 2b = 130$$

$$2(a + b) = 130$$

$$a + b = 65$$

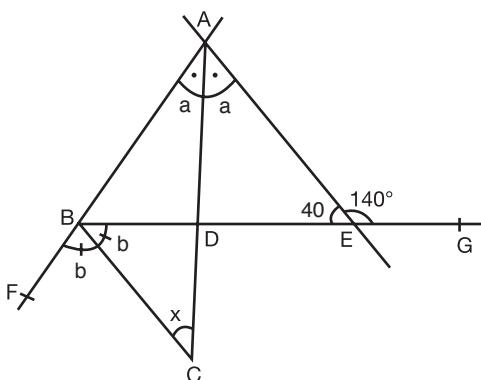
$$\underbrace{x + a + b}_{65} = 180^\circ$$

$$x = 115^\circ$$

Cevap: C

TASARI & DEV KADRO

9.



I. yol:

$$x = \frac{m(\widehat{AEB})}{2} = \frac{40}{2} = 20^\circ$$

II. yol:

$$2a + 40 = 2b \Rightarrow 2b - 2a = 40 \quad (\widehat{AEB})$$

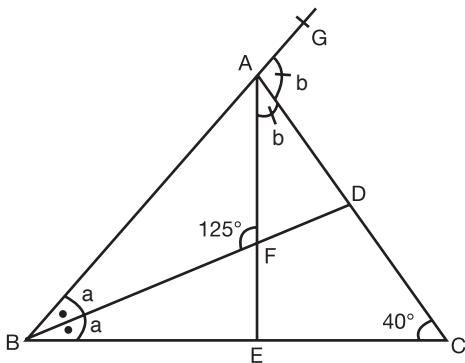
$$b - a = 20$$

$$a + x = b \Rightarrow x = b - a = 20^\circ \quad (\widehat{ABC})$$

Cevap: B

AÇI – ÜÇGENDE AÇI

10.



$$\bullet 2a + 40 = b \quad (\widehat{ABC})$$

$$\bullet a + b + 125 = 180$$

$$a + b = 85$$

$$b = 85 - a$$

$$\Rightarrow 2a + 40 = 85 - a$$

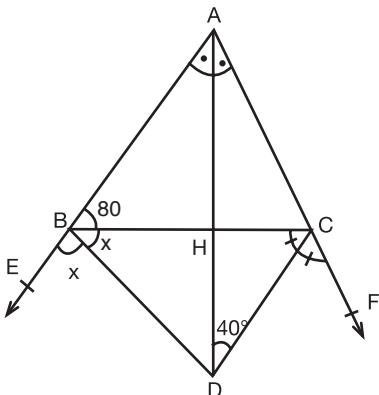
$$3a = 45$$

$$a = 15$$

$$m(\widehat{ABC}) = 2a = 30^\circ$$

Cevap: E
TASARI & DEV KADRO

11.

**Kural:**

[AD] ve [CD] açıortay ise [BD]'de açıortaydır.

$$m(\widehat{ADC}) = \frac{m(\widehat{ABC})}{2} \Rightarrow 40 = \frac{m(\widehat{ABC})}{2}$$

$$\Rightarrow m(\widehat{ABC}) = 80^\circ$$

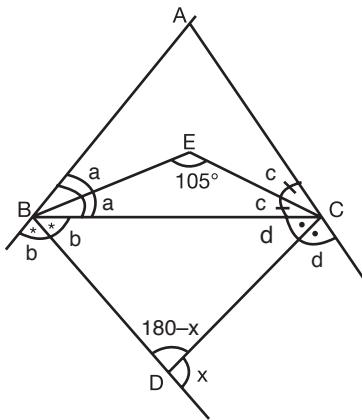
$$2x + 80 = 180^\circ$$

$$2x = 100^\circ$$

$$x = 50^\circ$$

Cevap: C

12.



$$2a + 2b = 180$$

$$a + b = 90$$

$$2c + 2d = 180$$

$$c + d = 90$$

EBCD dörtgeninin iç açıları toplamı 360° dir.

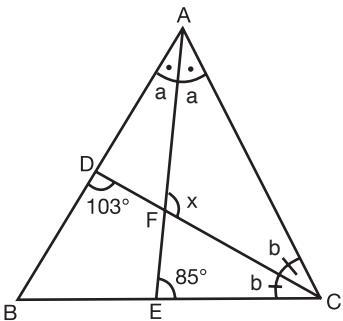
$$105 + 90 + 90 + 180 - x = 360$$

$$x = 105^\circ$$

Cevap: A

ÜÇGENDE AÇI

1.



$$2a + b = 103 \text{ (}\widehat{\text{ADC}}\text{)}$$

$$a + 2b + 85 = 180 \text{ (}\widehat{\text{AEC}}\text{)} \Rightarrow a + 2b = 95$$

$$2a + b = 103$$

$$+ \quad a + 2b = 95$$

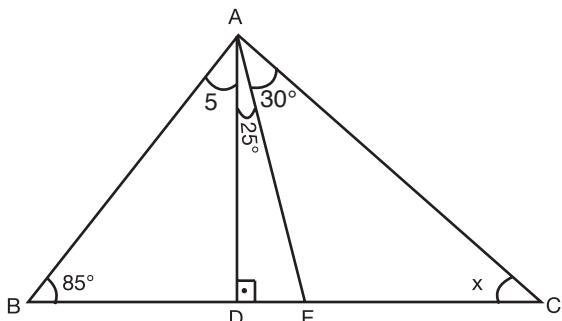
$$3a + 3b = 198 \Rightarrow 3(a + b) = 198 \text{ olur.}$$

$$a + b = 66$$

$$\underbrace{a + b}_{66} + x = 180 \text{ (}\widehat{\text{AFC}}\text{)}$$

$$66 \quad x = 114^\circ$$

3.



I. yol:

$$m(\widehat{\text{BAE}}) = m(\widehat{\text{EAC}}) = 30^\circ$$

$$x + 55 + 90 = 180$$

$$x = 35^\circ$$

II. yol:

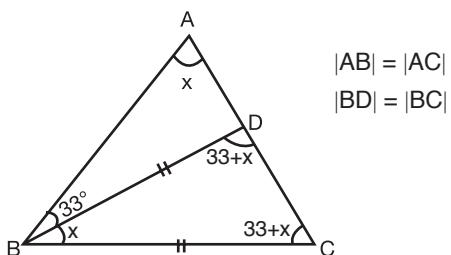
$$m(\widehat{\text{DAE}}) = \frac{|m(\widehat{\text{B}}) - m(\widehat{\text{C}})|}{2}$$

$$25 = \frac{|85 - x|}{2}$$

$$x = 35$$

Cevap: B

2.



$$|AB| = |AC|$$

$$|BD| = |BC|$$

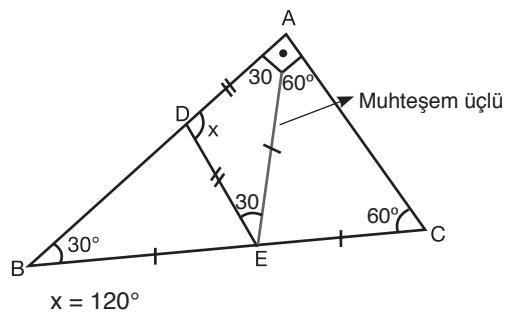
$$x + (33 + x) + (33 + x) = 180^\circ$$

$$3x = 114$$

$$x = 38^\circ$$

Cevap: A

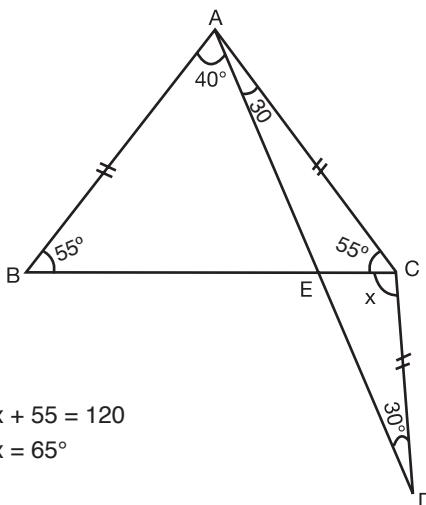
4.



Cevap: D

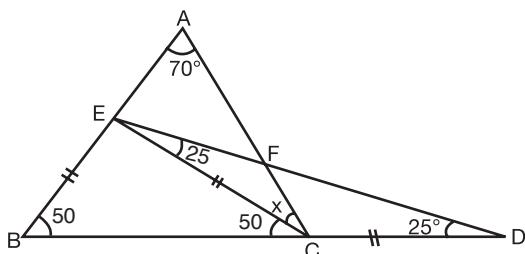
ÜÇGENDE AÇI

5.



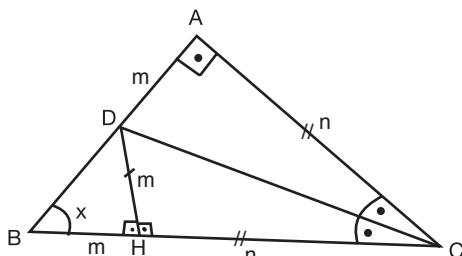
Cevap: A

6.



Cevap: B

7.

**Kural**

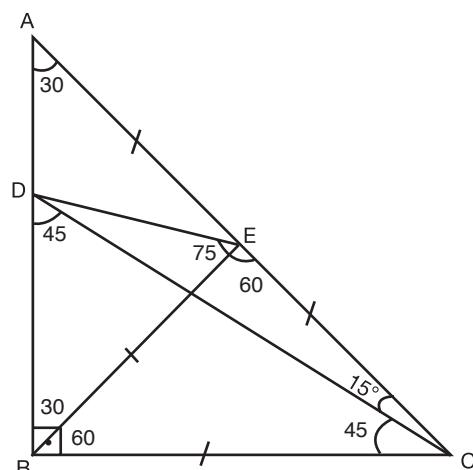
Açıortay üzerinden kollara indirilen dikmelerin uzunlukları ve açıortay kollarının uzunlukları birbirine eşittir.

$m = |AD| = |DH|$ ve $n = |AC| = |HC|$ dir.

Dolayısıyla $|BH| = m$ dir. Yani $\triangle BDH$ üçgeni ikizkenar dik üçgendir. $x = 45^\circ$

Cevap: D

8.



$\triangle BDC$ ikizkenar dik üçgen $|DB| = |BC|$

$\triangle DBE$ ikizkenar üçgen $|DB| = |BE|$

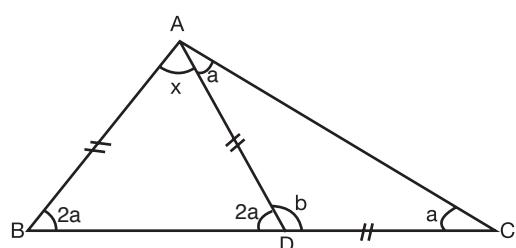
$$m(\widehat{DBE}) = 30 \Rightarrow m(\widehat{DBE}) = m(\widehat{DEB}) = 75^\circ$$

$$x = 60^\circ + 75^\circ = 135^\circ$$

Cevap: E

TASARI & DEV KADRO

9.



$$\begin{aligned} 2a + b &= 180 \\ + b - 2a &= 48 \\ \hline 2b &= 228 \\ b &= 114 \text{ ve } a = 33 \end{aligned}$$

$$4a + x = 180$$

$$4 \cdot 33 + x = 180$$

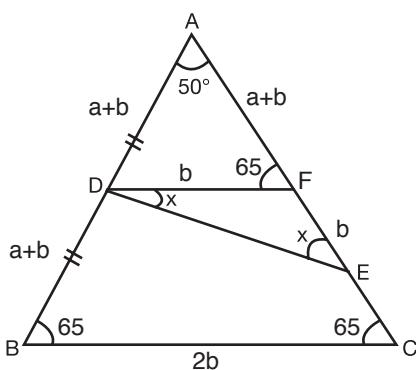
$$x = 180 - 132$$

$$x = 48^\circ$$

Cevap: D

ÜÇGENDE AÇI

10.



$$|AB| = |AC| = 2a + 2b$$

$$|EC| + |BC| = |AE|$$

$$a \quad 2b \quad a+2b$$

[DF] orta taban

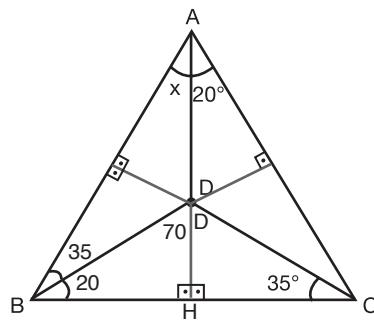
$$|DF| = \frac{|BC|}{2} = b$$

$$2x = 65 \Rightarrow x = 32,5^\circ$$

Cevap: B

TASARI & DEV KADRO

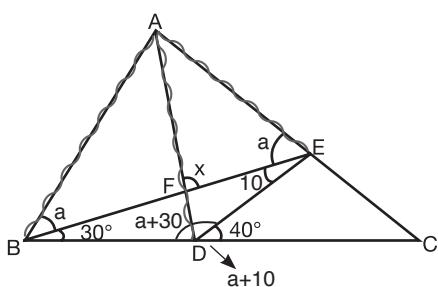
12.



$$x = 35^\circ \quad (\widehat{ABH})$$

Cevap: A

11.



$$(a + 30) + (a + 10) + 40 = 180$$

$$2a + 80 = 180$$

$$2a = 100$$

$$a = 50$$

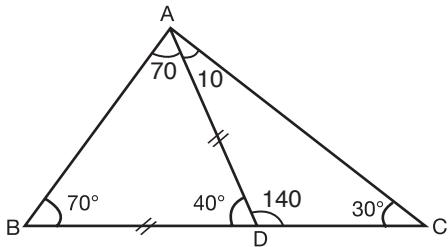
$$x = a + 10 + 10$$

$$x = 70^\circ$$

Cevap: E

AÇI - KENAR BAĞINTILARI

1.

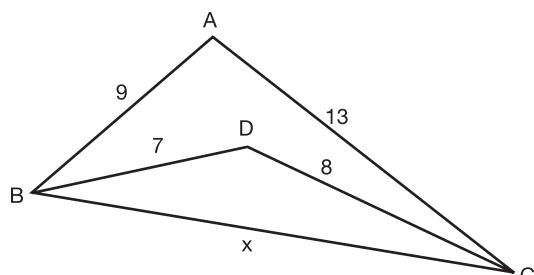
 \widehat{ABD} için $|AD| = |BD| > |AB|$ \widehat{ADC} için $|AC| > |AD| > |DC|$ \widehat{ABC} için $|BC| > |AC| > |AB|$

Sonuç olarak;

 $|BC| > |AC| > |AD| = |BD| > |AB|$ ve $|AD| > |DC|$ dir. $|DC| > |AD|$ ifadesi yanlışır.

Cevap: C

3.

 \widehat{ABC} iken $|13 - 9| < x < |13 + 9|$
 $4 < x < 22$ \widehat{BDC} iken $|8 - 7| < x < |18 + 7|$
 $1 < x < 15$

Sonuç olarak

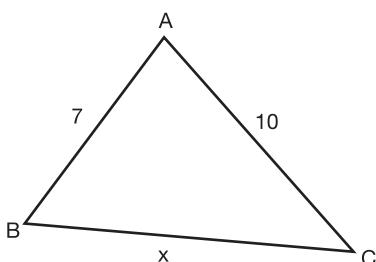
 $4 < x < 15$ olmalıdır. (En dar aralık seçilir.)

x'in alabileceği 10 farklı değer vardır.

Cevap: A

TASARI & DEV KADRO

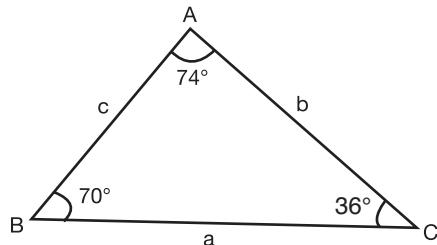
2.

Genel kurala göre $3 < x < 17$ $m(\widehat{B}) < m(\widehat{A})$ için $10 < x$ Sonuç olarak $10 < x < 17$ olmalıdır.

x'in alabileceği 6 farklı değer vardır.

Cevap: B

4.

 $c < b < a'$ dir.

$$|a - b| - |b - c| - |c - a|$$

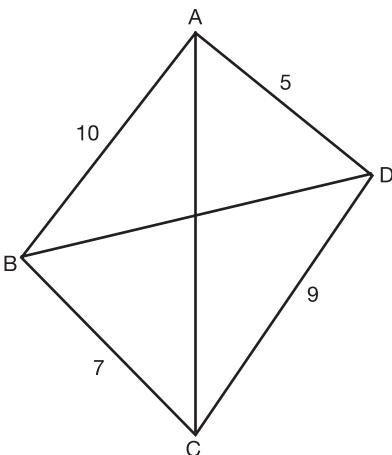
 $\downarrow \quad \downarrow \quad \downarrow$
 $b < a \quad c < b \quad c < a$

$$(a - b) - (b - c) - (a - c) = a' - b - b + c - a' + c \\ = 2c - 2b$$

Cevap: E

AÇI - KENAR BAĞINTILARI

5.

 \widehat{ABD} için $5 < |BD| < 15$ \widehat{BCD} için $2 < |BD| < 16$ Sonuç olarak $5 < |BD| < 15$ olmalıdır. \widehat{ABC} için $3 < |AC| < 17$ \widehat{ADC} için $4 < |AC| < 14$ Sonuç olarak $4 < |AC| < 14$ olmalıdır.

$$5 < |BD| < 15$$

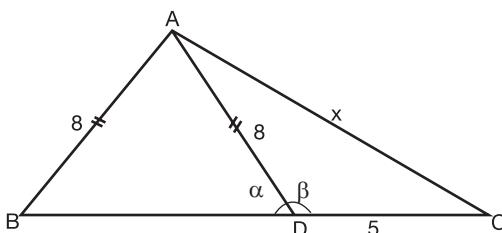
$$+ \quad 4 < |AC| < 14$$

$$9 < |BD| + |AC| < 29$$

 $|BD| + |AC|$ 'nin alabileceği en büyük değer 28 dir.

Cevap: C

6.

 $\alpha < 90^\circ$ olmalıdır. Dolayısıyla $\beta > 90^\circ$ dir. Yani \widehat{ADC} 'ni geniş açılı üçgendir.

$$8^2 + 5^2 < x^2 \quad \text{ve} \quad 3 < x < 13$$

$$89 < x^2$$

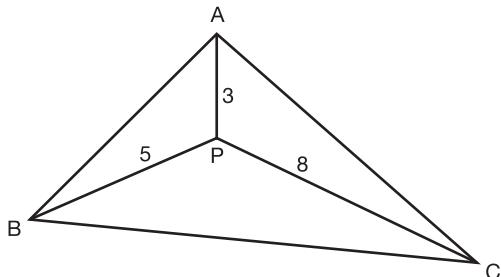
$$\sqrt{89} < x$$

Sonuç olarak $\sqrt{89} < x < 13$ tür.

x'in alabileceği en küçük değer 10'dur.

Cevap: B

7.



Kural

$$|AP| + |BP| + |CP| < \angle(ABC) < 2 \cdot (|AP| + |BP| + |CP|)$$

$$3 + 5 + 8 < \angle(ABC) < 2 \cdot (3 + 5 + 8)$$

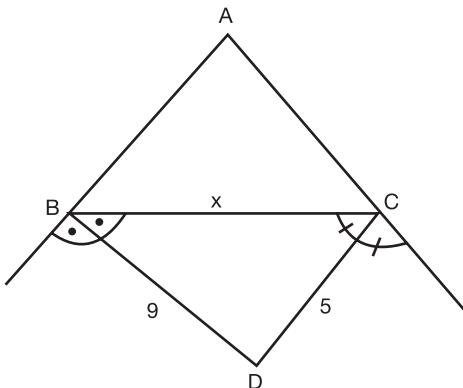
$$16 < \angle(ABC) < 32 \text{ olmalıdır.}$$

 $\angle(ABC) = 33$ olamaz.

Cevap: E

TASARI & DEV KADRO

8.

 $m(\widehat{D}) = 90 - \frac{m(\widehat{A})}{2}$ dir. Yani \widehat{D} dar açıdır.

Buna göre

$$x^2 < 9^2 + 5^2 \quad \text{ve} \quad 4 < x < 13$$

$$x^2 < 106$$

$$x < \sqrt{106}$$

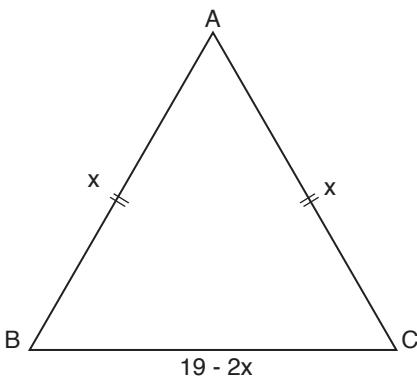
Sonuç olarak $4 < x < \sqrt{106}$ ($\sqrt{106} = 10, \dots$)

x'in alabileceği tamsayı değerleri 5, 6, 7, 8, 9, 10'dur.

Cevap: B

AÇI - KENAR BAĞINTILARI

9.



$$|19 - 2x - x| < x < |19 - 2x + x|$$

$$\begin{array}{c} \text{I. } |19 - 3x| < x < |19 - x| \\ \text{II. } \end{array}$$

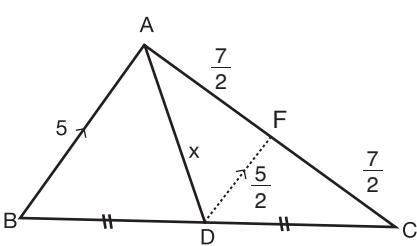
$$\begin{array}{ll} \text{I. için } 19 - 3x < x & \text{II. için } x < 19 - x \\ 19 < 4x & 2x < 19 \\ \frac{19}{4} < x & x < \frac{19}{2} \end{array}$$

$$\text{Sonuç olarak } \frac{19}{4} < x < \frac{19}{2}$$

4. ... < x < 9.5 ...

x'in alabileceği tamsayı değerleri 5, 6, 7, 8, 9 dur.

10.



$[DF] // [AB]$ çizilir. (Orta taban)

$$|AF| = |FC| = \frac{7}{2}$$

$$|DF| = \frac{|AB|}{2} = \frac{5}{2} \text{ dir.}$$

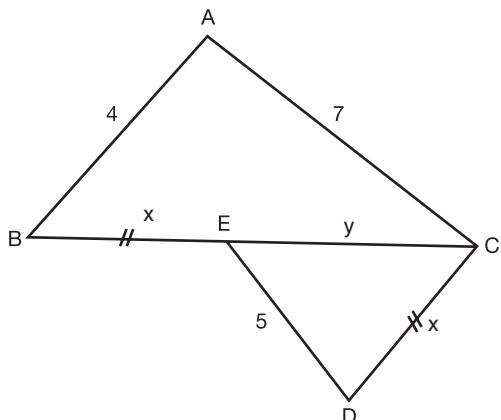
$$\widehat{\text{ADF}} \text{ için } \left| \frac{7}{2} - \frac{5}{2} \right| < x < \left| \frac{7}{2} + \frac{5}{2} \right|$$

x'in alabileceği tamsayı değerleri 2, 3, 4, 5 tir.

$$2 + 3 + 4 + 5 = 14 \text{ tür.}$$

Cevap: C

11.



$$\widehat{\text{ABC}} \text{ için } |7 - 4| < |BC| < |7 + 4|$$

$$3 < |BC| < 11 \text{ dir.}$$

$$3 < x + y < 11$$

$$\widehat{\text{EDC}} \text{ için } |x - y| < 5 < |x + y|$$

Sonuç olarak $5 < x + y < 11$ olmalıdır.

$$5 < |BC| < 11$$

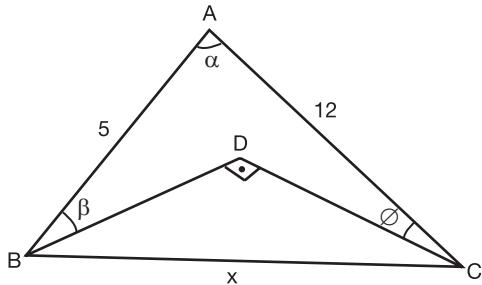
$|BC|$ 'nin alabileceği 5 farklı değer vardır.

Cevap: A

TASARI & DEV KADRO

Cevap: E

12.



$$\alpha + \beta + \theta = 90^\circ \text{ olduğundan } \alpha < 90^\circ \text{ diyebiliriz.}$$

Yani $\widehat{\text{ABC}}$ üçgeni dar açılı üçgendir.

$$x^2 < 5^2 + 12^2 \quad \text{ve} \quad |12 - 5| < x < |12 + 5|$$

$$x^2 < 169$$

$$x < \sqrt{169}$$

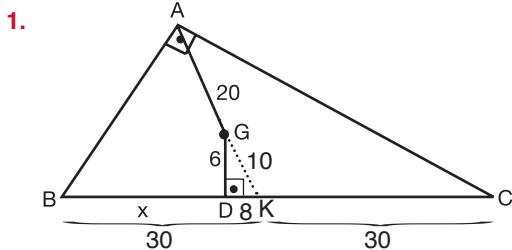
$$x < 13$$

Sonuç olarak

$7 < x < 13$ olmalıdır. x'in alabileceği en büyük tamsayı değeri 12'dir.

Cevap: E

KENARORTAY



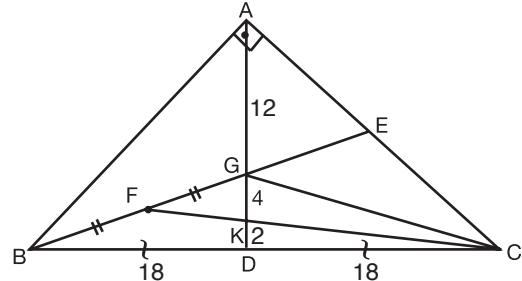
$$|AG| = 2|GK| \Rightarrow |GK| = 10 \text{ br}$$

\widehat{GDK} üçgeninde $|DK| = 8 \text{ br}$ (6, 8, 10 üçgeni)

$m(\widehat{A}) = 90^\circ \Rightarrow |AK| = |BK| = |KC| = 30 \text{ br}$ (Muhteşem üçlü)

$x = 22 \text{ br}'\text{dir.}$

Cevap: E



BGC üçgeninde $[GD]$ ve $[FC]$ kenarortay olduğundan K noktası bu üçgenin ağırlık merkezidir.

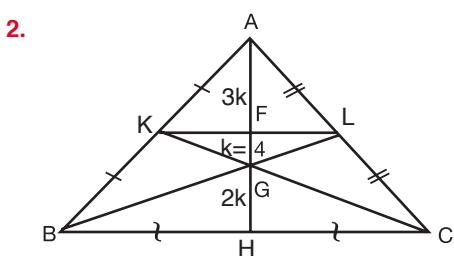
$$2|KD| = |GK| \Rightarrow |KD| = 2 \text{ br}$$

$$2|GD| = |AG| \Rightarrow |AG| = 12 \text{ br}$$

$m(\widehat{A}) = 90^\circ$ ve $|AD| = 18 \text{ br} \Rightarrow |BC| = 36 \text{ br}$ (Muhteşem üçlü)

Cevap: E

TASARI & DEV KADRO



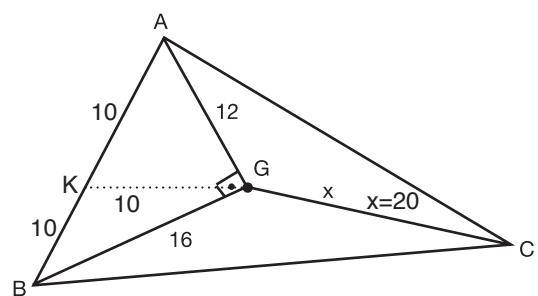
$k = 4$ ise $6k = 24$ 'tür.

Not: • $[KL]$ orta tabandır. Yani $|AF| = |FH|$

• G ağırlık merkezidir. Yani $2|GHI| = |AGI|$ 'dır.

Bu iki eşitliği sağlayan oran $(3k, k, 2k)$

Cevap: C

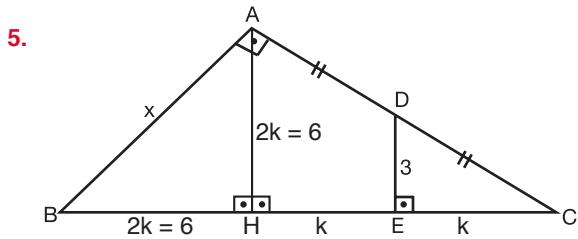


\widehat{ABD} için $|ABI| = 20 \text{ br}$ (12, 16, 20 üçgeni) $|GKI| = 10 \text{ br}$ (Muhteşem üçlü)

$$x = |GCI| = 2|GKI| = 20 \text{ br}$$

Cevap: D

KENARORTAY



$$4 \cdot IECI = IBCI$$

$IECI = k$ dersek $IBCI = 4k$ olur.

$[AH]$ dikmesini indirirsek $IHEI = IECI = k$ olur.

Dolayısıyla $IBHI = 2k$ olur. (\widehat{AHC})

\widehat{ABC} de $m(\widehat{A}) = 90^\circ$ ve $IBHI = IHCI$ olduğundan

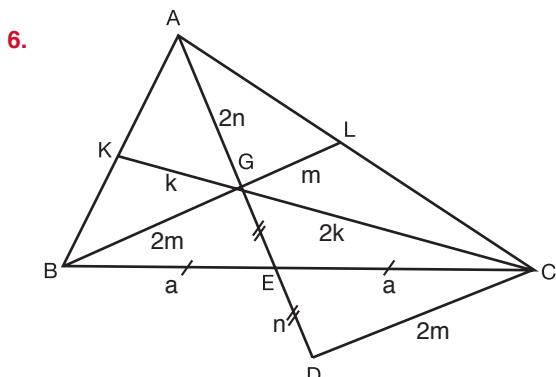
$IAHI = 2k$ olur. (Muhteşem üçlü)

\widehat{AHC} de $IAHI = 2 \cdot IDEI$ olduğundan $IAHI = 6$ br

\widehat{ABH} üçgeni ikizkenar dik üçgendir.

$$x = 6\sqrt{2} \text{ br'dir.}$$

Cevap: C



$$IAEI + IBLI + IKCI = 36 \text{ br}$$

$$IGEI = IEDI$$

$$3k + 3m + 3n = 36$$

$$3(k + m + n) = 36$$

$$k + m + n = 12 \text{ br}$$

\widehat{EBG} ve \widehat{ECD} üçgenleri eş üçgenleri
(Kenar - Açı - Kenar)

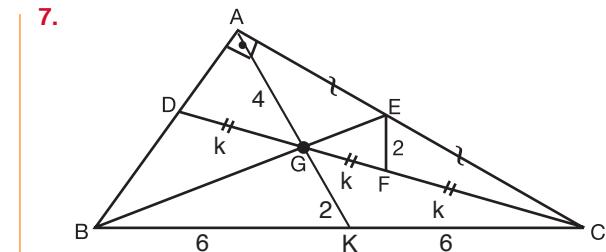
Dolayısıyla $IDCI = 2m$ br'dır.

$$\mathcal{C}(GDC) = 2k + 2m + 2n$$

$$= 2(k + m + n)$$

$$= 2 \cdot 12$$

$$= 24 \text{ br'dir.}$$



$$IDGI = IFCI = k \text{ dersek}$$

$$2 \cdot IDGI = IGCI \text{ olduğundan } IGF = k \text{ olur.}$$

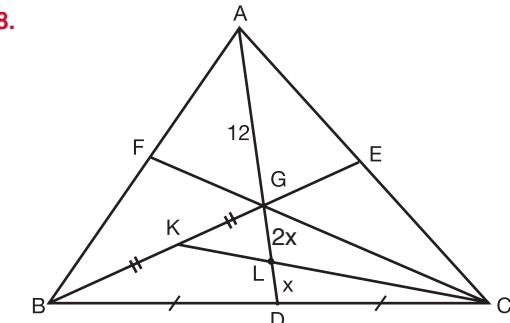
AGC üçgeninde $[EF]$ orta taban olduğundan $IADI = 4$ br'dir. $IGKI = 2$ br ve $IAKI = 6$ br olur.

$$IBCI = 2 \cdot IAKI \text{ (Muhteşem üçlü)}$$

$$IBCI = 2 \cdot 6 = 12 \text{ br}$$

Cevap: C

TASARI & DEV KADRO



BGC üçgeninde $[KC]$ ve $[GD]$ kenarortay olduğundan L noktası bu üçgenin ağırlık noktasıdır.

$$ILDI = x \Rightarrow IGLI = 2x \text{ tır.}$$

$$\text{ABC üçgeninde } IAGI = 12, \quad IGDI = 3x = 6 \text{ br}$$

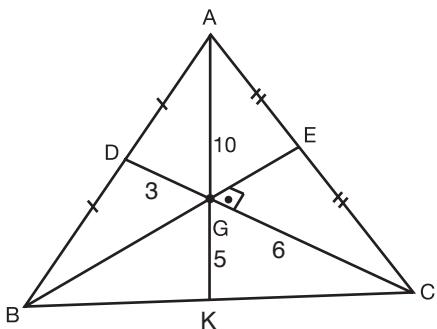
$$\Rightarrow x = 2 \text{ br'dir.}$$

Cevap: B

Cevap: A

KENARORTAY

9.



$V_b \perp V_c$ olduğundan $V_a^2 = V_b^2 + V_c^2$ 'dir.

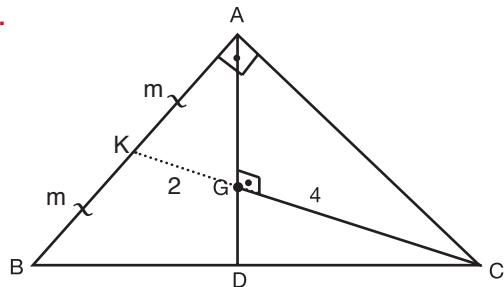
$$V_a = 15 \text{ br} \quad V_c = 9 \text{ br} \quad V_b = ?$$

$$15^2 = 9^2 + V_b^2$$

$$V_b^2 = 144 \Rightarrow V_b = IBEL = 12 \text{ br}'dir.$$

Cevap: C

11.



AKC üçgeninde öklid teoremi uygularsak

$$m^2 = 2(2+4) = 12$$

$$m^2 = 12$$

$$m = 2\sqrt{3}$$

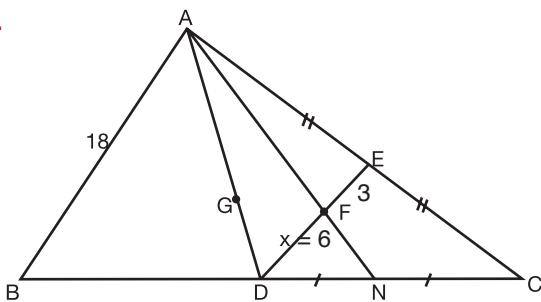
$$x = 2m = 2 \cdot 2\sqrt{3}$$

$$x = 4\sqrt{3}$$

Cevap: B

TASARI & DEV KADRO

10.



ADC üçgeninde F noktası ağırlık merkezidir.

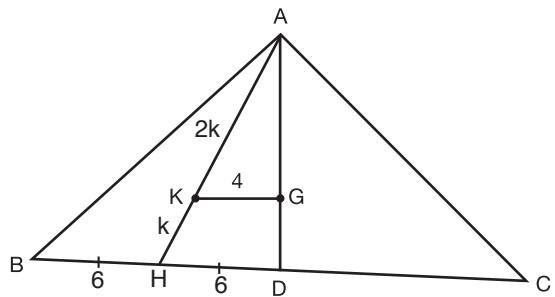
ABC üçgeninde [DE] orta tabandır.

$$|DE| = \frac{|AB|}{2} = 9 \text{ br}'dir. \quad |FE| = 3 \text{ br}$$

$$|DF| = X = 6 \text{ br}'dir.$$

Cevap: E

12.



AHD üçgeninde benzerlik uygularsak

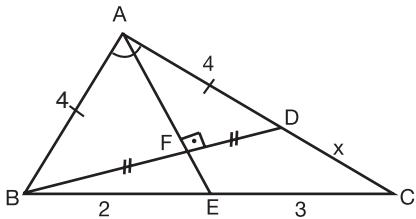
$$\frac{|AK|}{|AH|} = \frac{2k}{3k} = \frac{|KG|}{|HD|} \Rightarrow |HD| = 6 \text{ br}$$

$$|IBDI| = |IDCI| = 12 \text{ br} \Rightarrow |IBCI| = 24 \text{ br}'dir.$$

Cevap: D

AÇIORTAY

1.



ABC üçgeninde

[AF] yükseklik ve kenarortay ise aynı zamanda açıortaydır ve ABD üçgeni ikizkenar üçgendir.

$$|ABI| = |ADI| = 4 \text{ br}$$

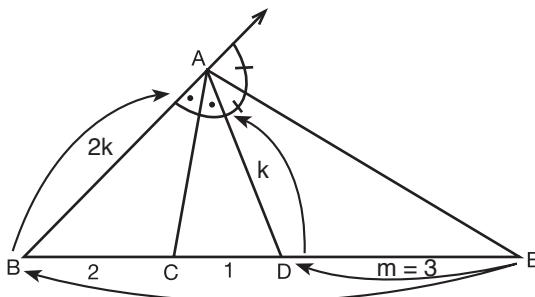
ABC üçgeninde iç açıortay teoremine göre

$$\frac{|AB|}{|BE|} = \frac{|AC|}{|EC|} \text{ dir. } \frac{4}{2} = \frac{4+x}{3} \Rightarrow x = 2 \text{ br}$$

Cevap: D

TASARI & DEV KADRO

2.



ABC üçgeninde iç açıortay teoremine göre

$$\frac{|AB|}{|AD|} = \frac{|BC|}{|CD|} = \frac{2}{1} \quad |AB| = 2k \text{ dersek} \\ |AD| = k \text{ olur.}$$

ABD üçgeninde dış açıortay teoremine göre

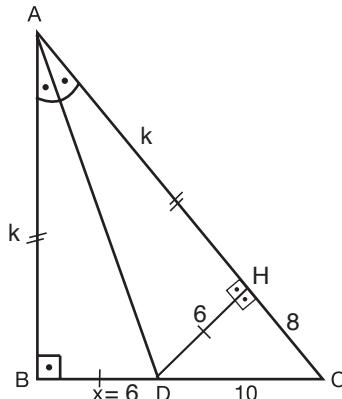
$$\frac{|DE|}{|BE|} = \frac{|AD|}{|AB|} = \frac{1}{2} \quad |DE| = m \text{ dersek} \\ |BE| = 2m \text{ olur.}$$

$$2m = 3 + m \Rightarrow m = 3 \text{ tür.}$$

$$\frac{|BC|}{|BE|} = \frac{2}{6} = \frac{1}{3}$$

Cevap: C

3.



$$|ABI| = k \text{ dersek } |AEI| = k + 8 \text{ olur.}$$

Açıortay üzerindeki aynı noktadan kollara indirilen dikmeler kolları aynı oranda böler ve uzunlukları eşittir. Dolayısıyla

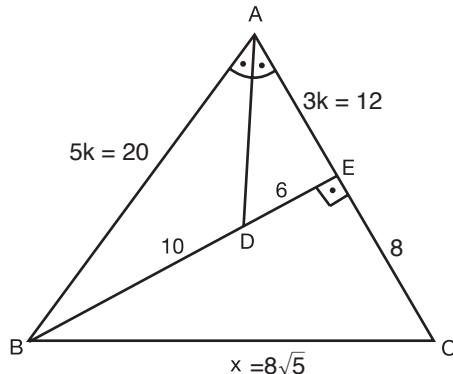
$$|ABI| = |AHI| = k \text{ ve } |IBD| = |IDH| = x \text{ dir.}$$

$$|IHC| = 8 \text{ ve } DHC \text{ dik üçgeninde } (6, 8, 10)$$

$$|IDH| = x = 6 \text{ br'dir.}$$

Cevap: C

4.



ABD üçgenin iç açıortay teoremine göre

$$\frac{|AB|}{|AE|} = \frac{|BD|}{|DE|} = \frac{10}{6} \text{ dir. } |AB| = 5k \text{ dersek} \\ |AE| = 3k \text{ olur.}$$

ABD dik üçgeni (12, 16, 20) üçgendir.

$$|ABI| = |ACI| \text{ olduğundan } |IEC| = 8 \text{ br'dir.}$$

EBC dik üçgeninde pisagor uygulanırsa

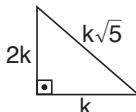
$$|IEB|^2 + |IEC|^2 = |IBC|^2$$

$$16^2 + 8^2 = x^2$$

$$x = 8\sqrt{5}$$

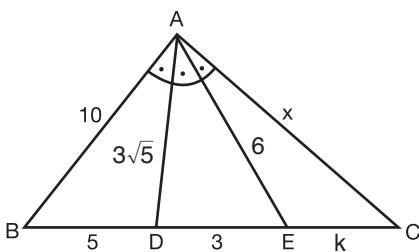
Cevap: D

Not:



AÇIORTAY

5.



ABE üçgeninde iç açıortay teoremine göre
 $|AE| = 6$ br'dir.
 ABE üçgeninde iç açıortay uzunluk teoremine göre
 $|ADI|^2 = |ABI| \cdot |AEI| - |IBD| \cdot |IDE|$

$$|ADI|^2 = 10 \cdot 6 - 5 \cdot 3 = 45$$

$$|ADI| = 3\sqrt{5}$$

ADC üçgeninde $\frac{|AD|}{|DE|} = \frac{|AC|}{|EC|} = \frac{3\sqrt{5}}{3} = \sqrt{5}$ 'tir.

$$|AC| = k\sqrt{5} \text{ dersen } |EC| = k \text{ olur.}$$

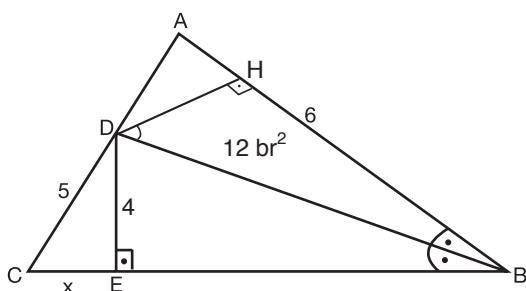
ADC üçgeninde iç açıortay uzunluk teoremine göre
 $|AEI|^2 = |ADI| \cdot |ACI| - |IDE| \cdot |IEC|$
 $6^2 = 3\sqrt{5} \cdot k\sqrt{5} - 3 \cdot k$

$$36 = 12k$$

$$k = 3 \quad x = k\sqrt{5} = 3\sqrt{5} \text{ 'dir.}$$

Cevap: C

6.



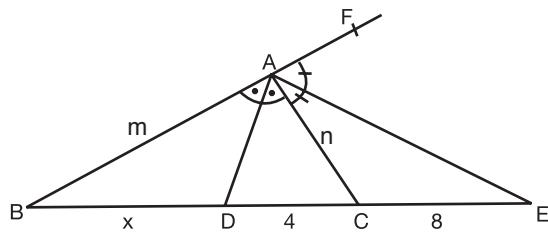
$$A(ABD) = 12 \text{ br}^2 \Rightarrow \frac{|DH| \cdot 6}{2} = 12 \text{ ve } |DH| = 4 \text{ br}$$

$|IDH| = |IDE|$ olduğundan $|IDE| = 4$ br'dir.

DEC üçgeni (3, 4, 5) üçgenidir. $x = 3$ br'dir.

Cevap: C

7.



ABC üçgenin iç açıortay teoremine göre

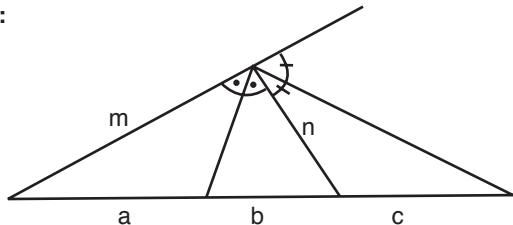
$$\frac{m}{n} = \frac{x}{4}$$

Dış açıortay teoremine göre $\frac{m}{n} = \frac{x+12}{8}$ 'dır.

$$\frac{x}{4} = \frac{x+12}{8} \Rightarrow x = 12 \text{ br'dir.}$$

Cevap: D

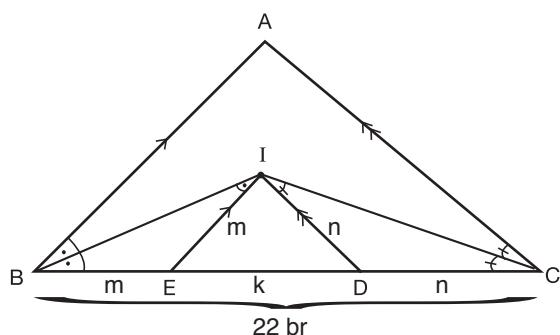
Not:



$$\frac{a-b}{a+b} = \frac{b}{c} \text{ dir. } \left(\frac{x-4}{x+4} = \frac{4}{8}, x = 12 \text{ br} \right)$$

TASARI & DEV KADRO

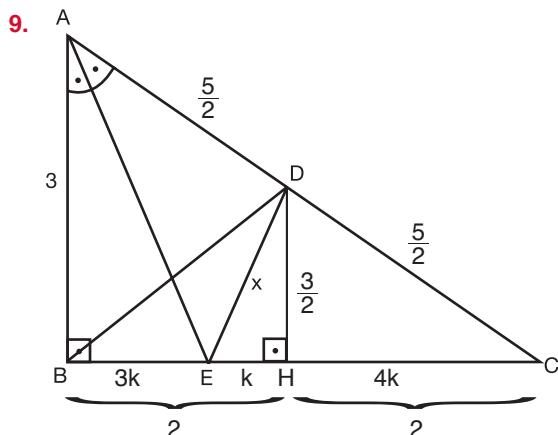
8.



$m + k + n = 22$ br ve $\angle IED = m + k + n$ olduğundan $\angle IED = 22$ br'dir.

Cevap: A

AÇIORTAY



$$m(\hat{B}) = 90^\circ \text{ ve } IBDI = IADI = \frac{5}{2} \Rightarrow IDC = \frac{5}{2}$$

(Muhteşem üçlü)

ABC dik üçgeni (3, 4, 5) üçgenidir.

$$|DH| = \frac{3}{2} \text{ dir.}$$

(Orta taban olduğundan) $|IBHI| = |IHCI| = 2$ dir.

ABC üçgeninde iç açıortay teoremine göre

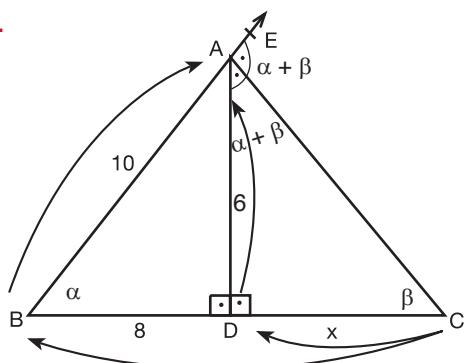
$$\frac{|AB|}{|AC|} = \frac{|BE|}{|EC|} = \frac{3}{5} \quad |BE| = 3k \text{ dersek} \\ |EC| = 5k \text{ olur.}$$

$$3k + 5k = 4 \Rightarrow k = \frac{1}{2}$$

DHE dik üçgenin pisagor uygulanırsa

$$x^2 = \left(\frac{3}{2}\right)^2 + \left(\frac{1}{2}\right)^2 = \frac{10}{4} \Rightarrow x = \frac{\sqrt{10}}{2} \text{ dir.}$$

10.



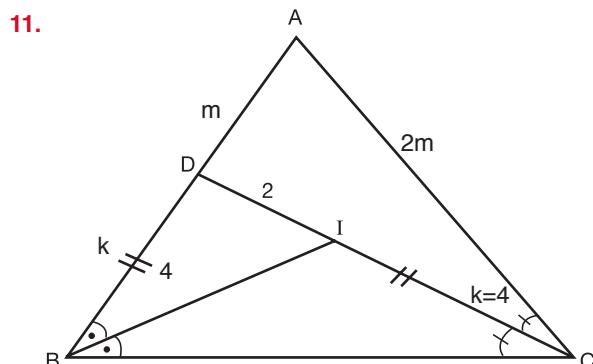
ABD dik üçgeni (6, 8, 10) üçgenidir. $|ADI| = 6$ br

ABC üçgeninde \widehat{EAC} dış açısı $m(\hat{B}) + m(\hat{C})$ eşit olduğundan $m(\widehat{EAC}) = \alpha + \beta$ dir.

ABD üçgeninde dış açıortay teoremine göre

$$\frac{x}{x+8} = \frac{6}{10} = \frac{3}{5} \quad 5x = 3x + 24 \\ 2x = 24 \\ x = 12 \text{ br'dir.}$$

Cevap: A



BDC üçgeninde iç açıortay teoremine göre

$$\frac{k}{2} = \frac{8}{k} \quad k^2 = 16 \Rightarrow k = 4 \text{ tür.}$$

ABC üçgeninde iç açıortay teoremine göre

$$\frac{|BC|}{|BD|} = \frac{|AC|}{|AD|} = \frac{8}{4} = 2 \quad |AC| = 2m \text{ dersek} \\ |AD| = m \text{ olur.}$$

ABC üçgeninde iç açıortay uzunluk teoremine göre

$$IDC^2 = IACI \cdot IBCI - IADI \cdot IBDI$$

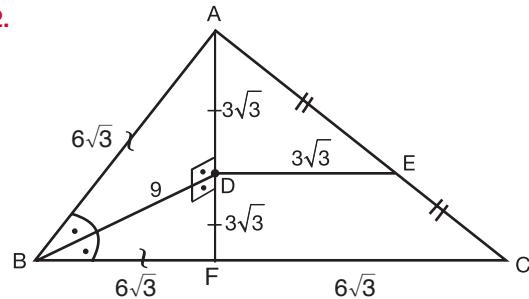
$$6^2 = 2m \cdot 8 - m \cdot 4$$

$$36 = 12m \quad x = 2m = 6 \text{ br}$$

Cevap: B

TASARI & DEV KADRO

12.



[AF] uzunluğu çizilirse

AFC üçgeninde [DE] orta taban olur.

$$2 \cdot IDEI = IFCI \Rightarrow IFCI = 6\sqrt{3}, IBFI = 6\sqrt{3} \text{ olur.}$$

ABF üçgeninde [BD] hem açıortay hem kenarortay olduğundan aynı zamanda yükseklik olur.

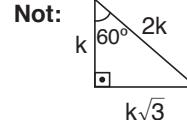
ABF üçgeni ikizkenar üçgen olmuş olur.

$$|ABI| = |IBF| = 6\sqrt{3} \text{ tür.}$$

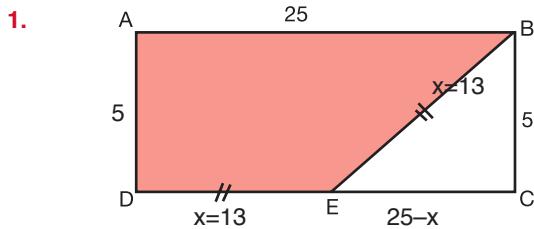
ABD üçgeninde pisagor uygulanırsa $|ADI| = 3\sqrt{3}$ olduğu görüldür. ABD üçgeni (30, 60, 90) üçgenidir.

$$m(\widehat{ABD}) = 30^\circ \text{ dir.}$$

Cevap: C



DİK ÜÇGEN

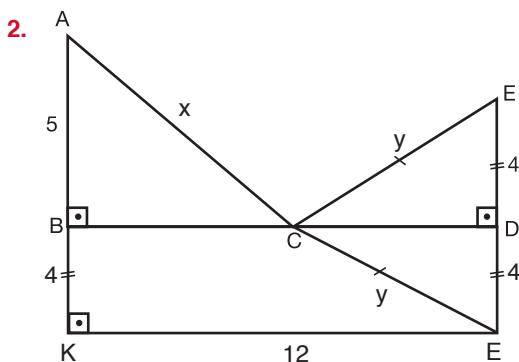


BEC üçgeni (5, 12, 13) üçgenidir.

$x = 13$ 'tür.

$$\mathcal{C}(\text{ADEB}) = 5 + 25 + 13 + 13 = 56 \text{ br}$$

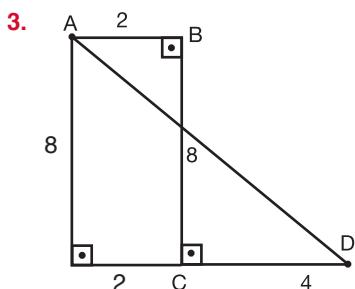
Cevap: E



AKE üçgeni (9, 12, 15) üçgenidir.

$$|AC| + |CE| = x + y = 15 \text{ dir.}$$

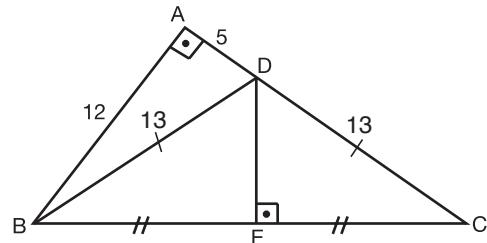
Cevap: C



AHD üçgeni (6, 8, 10) üçgenidir.

$$|AD| = 10 \text{ br'dir.}$$

Cevap: B



ABD üçgeni (5, 12, 13) üçgenidir.

DBC üçgeninde [DE] hem yükseklik, hem kenarortay olduğundan DBC üçgeni ikizkenar üçgendir.

$$|DC| = 13 \text{ br}$$

ABC dik üçgeninde pisagor uygularsak

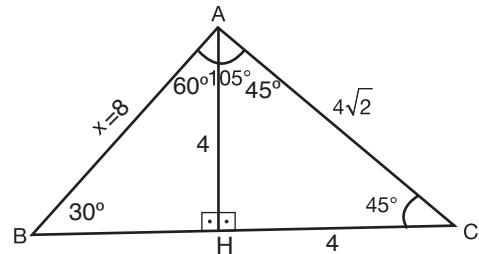
$$12^2 + 18^2 = |BC|^2$$

$$468 = |BC|^2$$

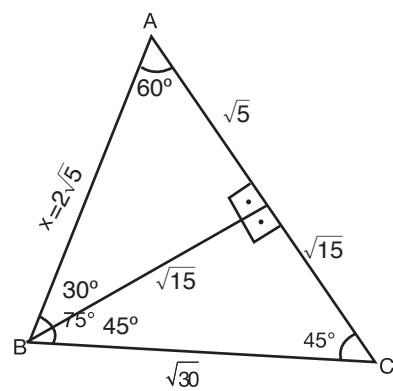
$$|BC| = 6\sqrt{13} \text{ 'tür.}$$

Cevap: C

TASARI & DEV KADRO

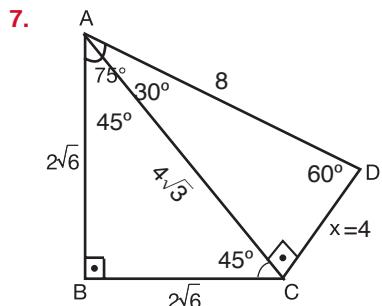


Cevap: E

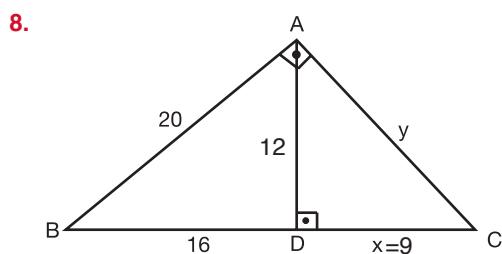


Cevap: A

DİK ÜÇGEN



Cevap: D

ABD üçgeni $(12, 16, 20)$ üçgenidir. $|ADI| = 12$ br.

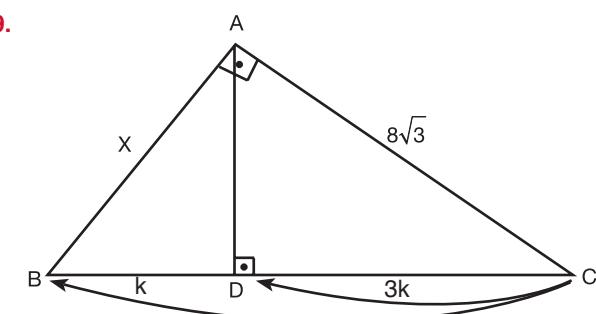
ABC üçgeninde öklid teoremi gereği

$$12^2 = 16 \cdot x \Rightarrow x = 9 \text{ br}$$

ADC üçgeni $(9, 12, 15)$ üçgenidir. $|ACI| = y = 15$ br'dir.

$$x + y = 9 + 15 = 24 \text{ br'dir.}$$

Cevap: D

 \widehat{ABC} 'de öklid teoremi gereği

$$(8\sqrt{3})^2 = 3k \cdot 4k$$

$$192 = 12k^2$$

$$k^2 = 16$$

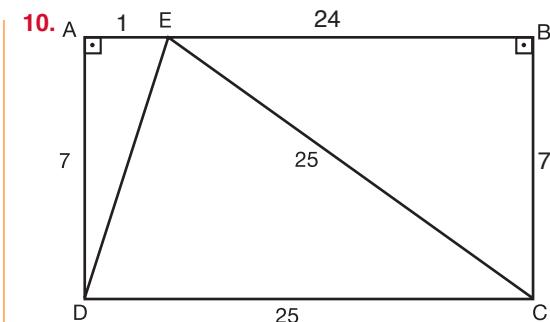
 $k = 4$ br'dir.

$$x^2 = k \cdot 4k$$

$$x^2 = 4 \cdot 16 = 64$$

 $x = 8$ br'dir.

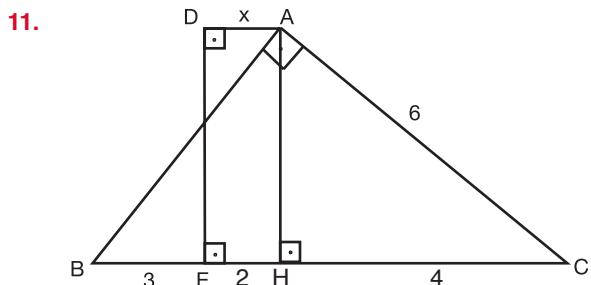
Cevap: C

 $\widehat{EBC} (7, 24, 25)$ üçgenidir. $|EBI| = 24$ br

$$|AEI| = 1 \text{ br'dir.}$$

Cevap: A

TASARI & DEV KADRO

 \widehat{ABC} 'de öklid gereği

$$|ACI|^2 = |HCI| \cdot |BCI|$$

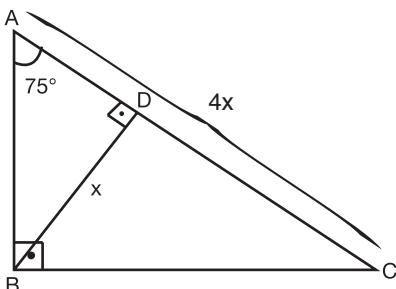
$$6^2 = |HCI| \cdot 9 \Rightarrow |HCI| = 4 \text{ br}$$

AHED dikdörtgeninde $|ADI| = |IEH| = x = 2$ br

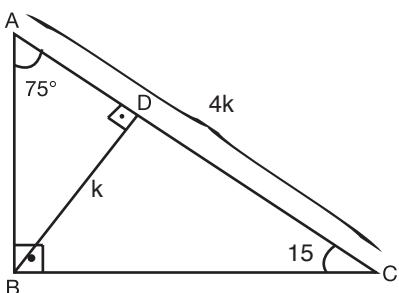
Cevap: B

DİK ÜÇGEN

12.



(15, 75, 90) üçgenin dik köşeden hipotenüze indirilen dikme hipotenüsün $\frac{1}{4}$ 'ne eşittir.
 $x + 4x = 25 \Rightarrow x = 5$ br'dır.

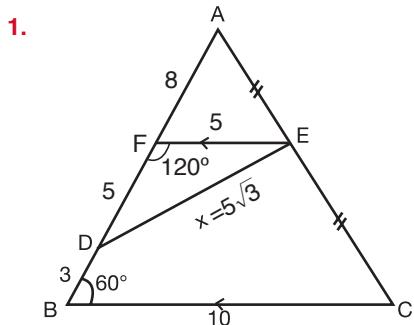
Not:

(15, 75, 90) üçgenin dik köşeden hipotenüze indirilen dikme hipotenüsün $\frac{1}{4}$ 'ine eşittir.

$x + 4x = 25 \Rightarrow x = 5$ br'dır.

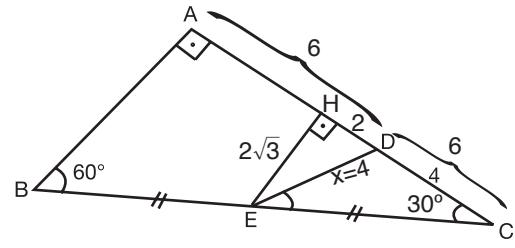
Cevap: B**TASARI & DEV KADRO**

ÖZEL ÜÇGENLER



$[EF]$ orta taban $|FB| = |FA| = 8$ br
ve $|EF| = \frac{|BC|}{2} = \frac{10}{2} = 5$ br'dır.
FDE üçgeni $(30, 30, 120)$ üçgendir.
 $x = 5\sqrt{3}$ 'tür.

Cevap: C

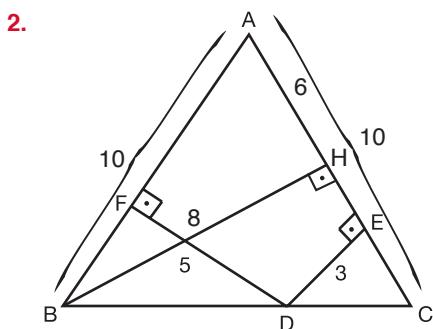


$[HE]$ orta taban olduğundan $|AH| = |HC| = 6$ br
ve $|HD| = 2$ br'dır.

HEC üçgeni $(30, 60, 90)$ 'dır.
 $|HCl| = 6$ br $\Rightarrow |HEI| = 2\sqrt{3}$ br
HED üçgeninde pisagor uygulanırsa
 $|HDI|^2 + |HEI|^2 = x^2$
 $2^2 + (2\sqrt{3})^2 = x^2$
 $x = 4$ br

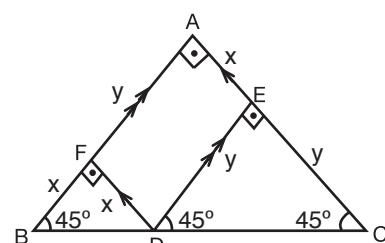
Cevap: B

TASARI & DEV KADRO



ABC ikizkenar üçgeninde
 $|BHI| = |FDI| + |EDI| = 5 + 3 = 8$ br'dır.
ABH üçgeni $(6, 8, 10)$ üçgendir.
 $|IAH| = 6$, $|HCI| = 4$ br'dır.
BHC üçgeninde pisagor uygulanırsa
 $|BHI|^2 + |HCI|^2 = |BCI|^2$
 $8^2 + 4^2 = |BCI|^2$
 $|BCI| = 4\sqrt{5}$ br'dır.

Cevap: E

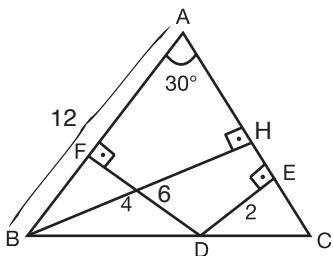


$x + y = 5\sqrt{2}$ br ve ABC ikizkenar dik üçgen olduğundan
 $|BCI| = (5\sqrt{2})\cdot\sqrt{2} = 10$ br'dır.

Cevap: E

ÖZEL ÜÇGENLER

5.



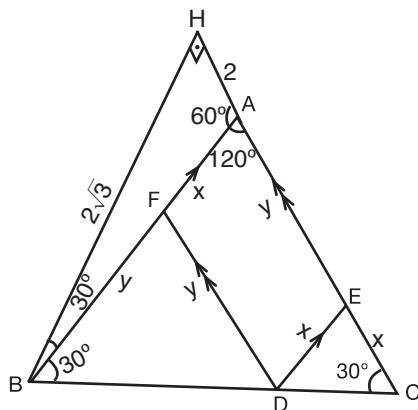
$$IBHI = IFDI + IDEI = 4 + 2 = 6 \text{ br}$$

ABH üçgeni (30, 60, 90) üçgenidir.

$$IBHI = 6 \text{ br} \Rightarrow IABI = 12 \text{ br}'\text{dir.}$$

Cevap: D

7.



B'nin [AC]'ye en kısa uzaklığı B'den AC'ye indirilen dikmenin uzunluğuudur. $IBHI = 2\sqrt{3}$ 'tür.

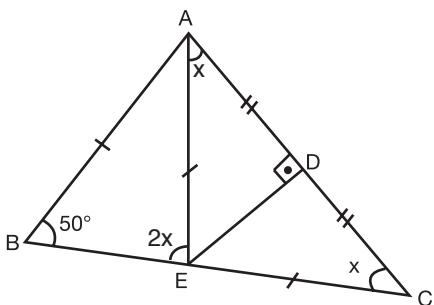
ABH üçgeni (30, 60, 90) üçgenidir.

$$IBHI = 2\sqrt{3} \Rightarrow IABI = x + y = IDEI + IDF = 4 \text{ br}'\text{dir.}$$

Cevap: C

TASARI & DEV KADRO

6.



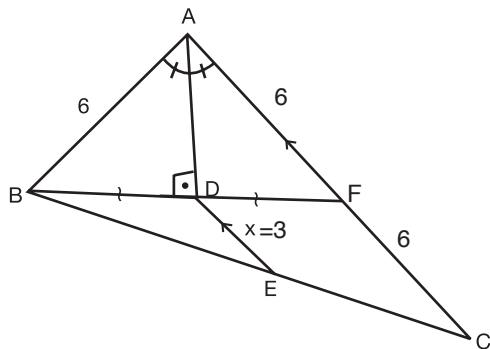
AEC ikizkenar üçgendir $|AE| = |EC|$

BAE ikizkenar üçgendir. $m(\hat{B}) = m(\hat{E})$

$$50 = 2x \Rightarrow x = 25^\circ$$

Cevap: A

8.



ABF üçgeni ikizkenardır. $|ABI| = |AFI| = 6 \text{ br}'\text{dir.}$

$$IFCI = 6 \text{ br olur.}$$

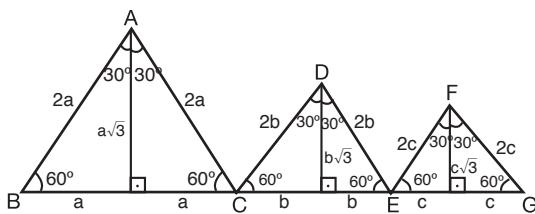
BFC üçgeninde $[DE] = x$ orta tabandır.

$$|DE| = \frac{|FC|}{2} = \frac{6}{2} = 3 \text{ br}'\text{dir.}$$

Cevap: C

ÖZEL ÜÇGENLER

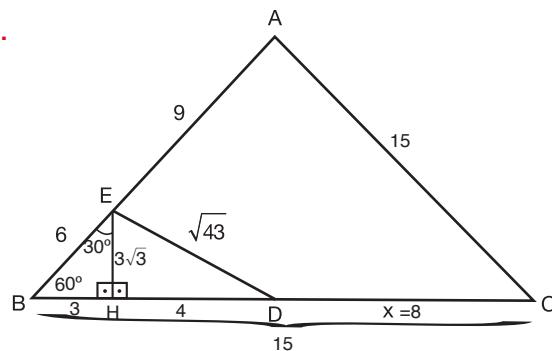
9.



$$\begin{aligned}
 a\sqrt{3} + b\sqrt{3} + c\sqrt{3} &= 4\sqrt{3} \Rightarrow \sqrt{3}(a + b + c) = 4\sqrt{3} \\
 a + b + c &= 4 \text{ tür.} \\
 \mathcal{C}(\text{ABC}) + \mathcal{C}(\text{DCE}) + \mathcal{C}(\text{FEG}) &= 6(a + b + c) \\
 &= 6 \cdot 4 \\
 &= 24 \text{ br'dir.}
 \end{aligned}$$

Cevap: D

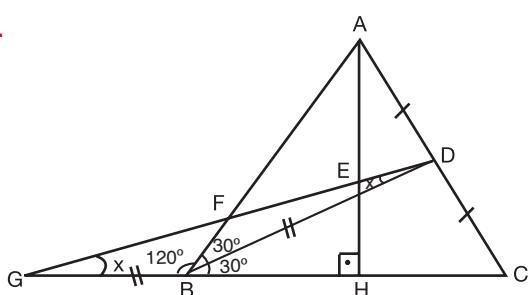
11.



Cevap: A

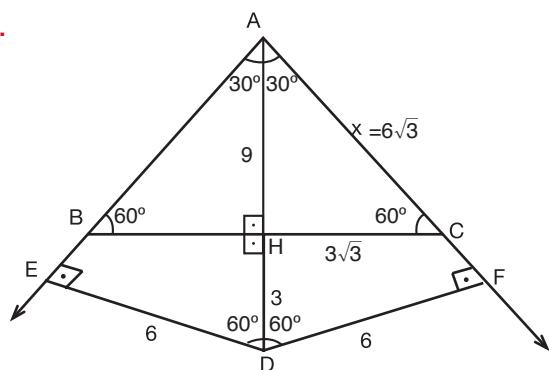
TASARI & DEV KADRO

10.

 $|AH| = |BD| = |GB|$ dir.GBD üçgeninde $m(B) = 150^\circ \Rightarrow x = 15^\circ$ dir.

Cevap: D

12.

AED ($30^\circ, 60^\circ, 90^\circ$) üçgeninde

IEDI = 6 br ise IADI = 12 br'dir. IAHI = 9 br'dir. AHC

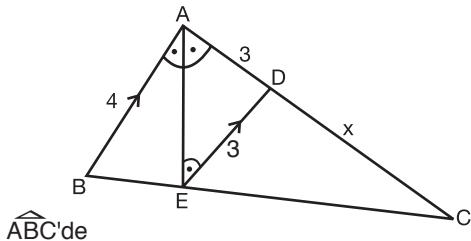
(30, 60, 90) üçgeninde

IAHI = 9 br ise IACI = x = $6\sqrt{3}$ br'dir.

Cevap: B

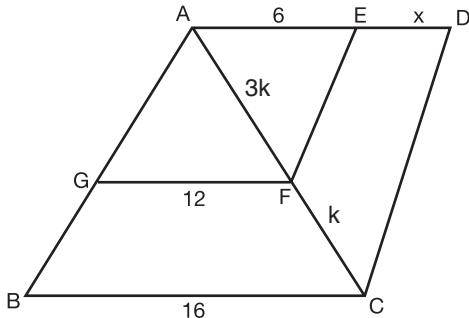
ÜÇGENDE BENZERLİK

1.



$$\widehat{ABC} \text{de } \frac{|DE|}{|AB|} = \frac{|CD|}{|AC|}, \quad \frac{3}{4} = \frac{x}{x+3} \Rightarrow x = 9 \text{ br}$$

3.



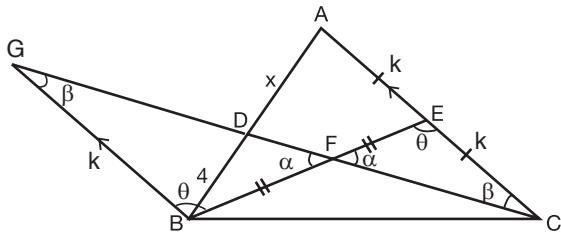
$$\widehat{ABC} \text{de } \frac{|GF|}{|BC|} = \frac{|AF|}{|AC|}, \quad \frac{12}{16} = \frac{3}{4}$$

$|AF| = 3k$ dersek $|AC| = 4k$ olur.

$$\widehat{ACD} \text{de } \frac{|AF|}{|FC|} = \frac{|AE|}{|ED|}, \quad \frac{3k}{k} = \frac{6}{x} \Rightarrow x = 2 \text{ dir.}$$

Cevap: B

2.



\widehat{GBD} üçgeni \widehat{FEC} üçgenine eşittir. $|GBI| = k$ br

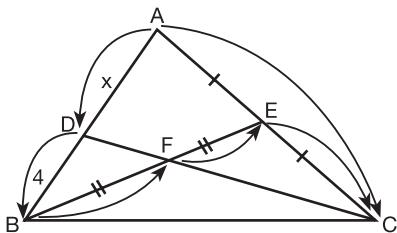
\widehat{GBD} ve \widehat{CAD} üçgenleri benzerdir.

$$\frac{|GB|}{|AC|} = \frac{|BD|}{|AD|}, \quad \frac{k}{2k} = \frac{4}{x} \Rightarrow x = 8 \text{ br'dir.}$$

Cevap: E

2. yol

Menelaus Teoremi

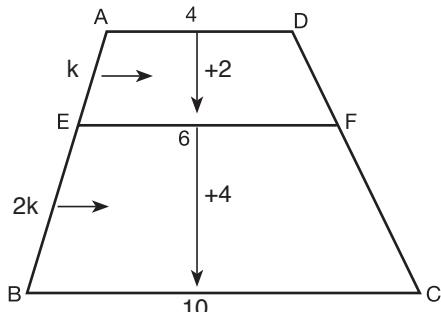


$$\frac{|EC|}{|AC|} \cdot \frac{|AD|}{|AB|} \cdot \frac{|BF|}{|FE|} = 1$$

$$\frac{1}{2} \cdot \frac{x}{4} \cdot \frac{1}{1} = 1 \quad x = 8 \text{ br}$$

TASARI & DEV KADRO

4.



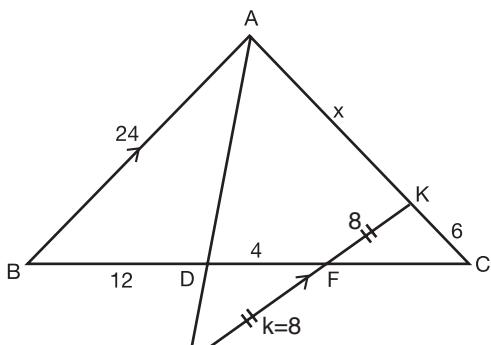
k da 2 br artarsa

$2k$ 'da 4 br artar $|BC| = 10$ br'dir.

Cevap: C

ÖZEL ÜÇGENLER

5.

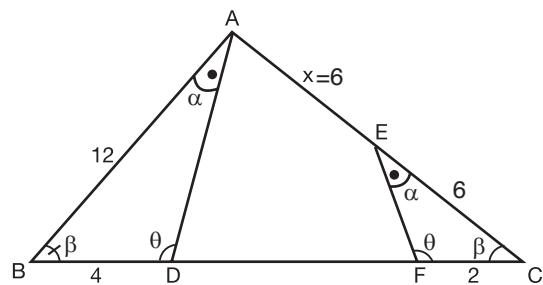


$$\frac{|DF|}{|BD|} = \frac{|EF|}{|AB|}, \frac{4}{12} = \frac{k}{24} \Rightarrow k = 8 \text{ dir.}$$

$$\widehat{\triangle ABC} \text{de } \frac{|KC|}{|AC|} = \frac{|KF|}{|AB|}, \frac{8}{24} = \frac{6}{6+x} \\ \Rightarrow x = 12 \text{ br'dir.}$$

Cevap: A

7.

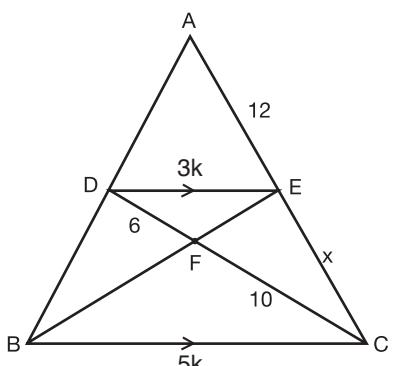
 $\widehat{\triangle ABD} \approx \widehat{\triangle ECF}$ 'dir.

$$\frac{|BD|}{|FC|} = \frac{|AB|}{|EC|}, \frac{4}{2} = \frac{12}{|EC|} \Rightarrow |EC| = 6 \text{ br}$$

 $|ABI| = |ACI| = 12 \text{ br}$ olduğundan $x = 6$ br'dir.

Cevap: C

6.



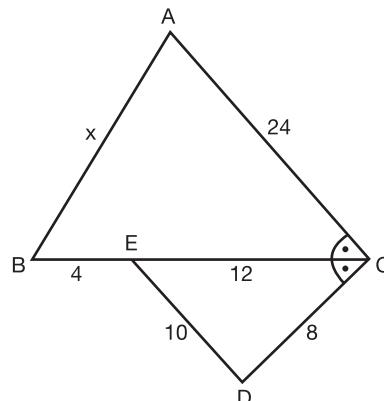
$$\frac{|DF|}{|FC|} = \frac{|DE|}{|BC|} = \frac{6}{10} \quad |DE| = 3k \text{ dersek} \\ |BC| = 5k \text{ olur.}$$

$$\widehat{\triangle ABC} \text{de } \frac{|DE|}{|BC|} = \frac{|AE|}{|AC|}, \frac{3k}{5k} = \frac{12}{12+x} \\ \Rightarrow 36 + 3x = 60 \\ 3x = 24 \\ x = 8$$

Cevap: D

TASARI & DEV KADRO

8.

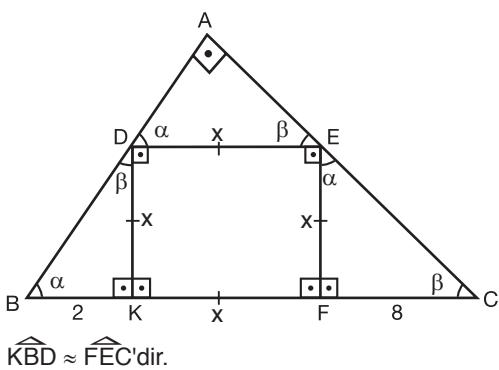
 $\widehat{\triangle CAB} \approx \widehat{\triangle ECD}$ (K. A. K)

$$\frac{|CA|}{|CE|} = \frac{|AB|}{|ED|} = \frac{|CB|}{|CD|} \Rightarrow \frac{24}{12} = \frac{x}{10} = \frac{16}{8} \\ x = 20$$

Cevap: E

ÖZEL ÜÇGENLER

9.

 $\widehat{KBD} \approx \widehat{FEC}$ dir.

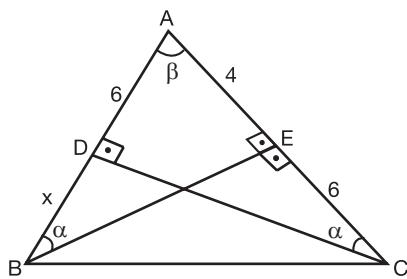
$$\frac{|BK|}{|EF|} = \frac{|DK|}{|FC|}, \frac{2}{x} = \frac{x}{8} \Rightarrow x^2 = 16$$

$x = 4$ br'dir.

$$A(DEFK) = x^2 = 16 \text{ br}^2$$

Cevap: C

11.

 $\widehat{EBA} \approx \widehat{DCA}$ dir.

$$\frac{|EA|}{|DA|} = \frac{|BA|}{|CA|}, \frac{\frac{2}{x}}{6} = \frac{x+6}{10}$$

$$20 = 3x + 18$$

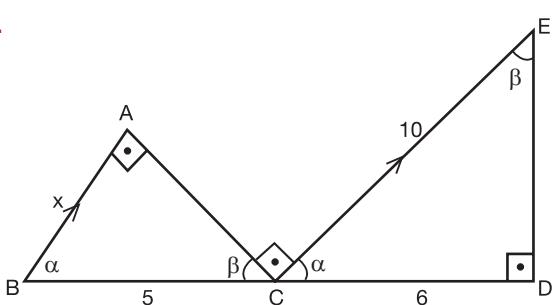
$$3x = 2$$

$$x = \frac{2}{3}$$

Cevap: A

TASARI & DEV KADRO

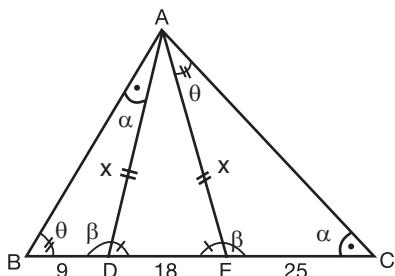
10.



$$\frac{|AB|}{|CD|} = \frac{|BC|}{|CE|}, \frac{x}{6} = \frac{5}{10} \Rightarrow x = 3 \text{ br}$$

Cevap: D

12.

 $\widehat{ADB} \approx \widehat{CEA}$

$$\frac{|BD|}{|EA|} = \frac{|AD|}{|CE|}, \frac{9}{x} = \frac{x}{25} \Rightarrow x^2 = 9.25$$

$x = 3\sqrt{0.25} = 1.5$

$$x = 15$$

$$C(ADE) = 2x + 18$$

$$= 30 + 18$$

$$= 48 \text{ br}$$

Cevap: D